Chapter No.8-17 Presented by: Urdu Books Whatsapp Group STUDY GROUP

9TH CLASS

0333-8033313 טוצוונ 0343-7008883 ياكستان زنده باد

0306-7163117 محد سلمان سليم Chapter #8:- Rana Mujeeb
"Linear Graphs and
their Applications."

Basic Concepts

- is Coodinate Plane.
- io Ordered Pair.
- iii) Coordinate Axes.
- iv) Abbaissa.
- vi) Ordinate. Instructor
 Rana Mujeeb
 vi) Origin. 0303-6058635
- vii) Quardrant.
- viii) Collinear Points.
- (v) Ex . 8.1.
- x) Ex . 8.2 , Q3 (only)
- xi) Conversion.

Instructor

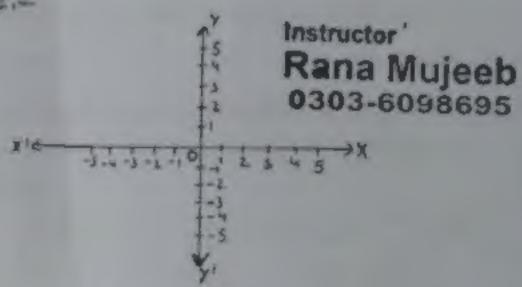
Rana Mujeeb 0303-6098695

Xiii) Review Ex 8. (without Q6).

Instructor' i) Coordinate Plane:- Rana Mujeeb

The plane formed by two straight lines perpendicular to each other is called coordinate plane and the lines are called coordinate CIRES.

Example:



iv Ordered Pair :-

An ordered pair is u pair of elements in which elements are written in specific order.

Example:-

(xxy), (0,-1), etc.

Instructor Rana Muleeb 0303-6098695

iii) Coordinate OIRES :-

The plane Formed by straight lines perpendicular to £ wa is called coordinate plane each other and the lines are called coordinate CHES.

Instructor Example:-Rana Mujeeb 0303-6098695

iv) Abbaisson :-

The x-coordinate of

point called abbaissa.

Example:-Instructor Rana Mujeeb

(3,4)

(3,4)

0303-6098695 Here, 3 15 a abbcissa.

v) Ordinate :-

The y coordinate is called

ordinate.

Example:-

Instructor Rana Mujeeb 0303-6098695

Hereily is a ordinate. vi) Origin:

The point of intersection of two coordinate axes is called origin. It is represented by "O"

Example:

Instructor

Rana Mujeeb

0303-6098695

vii Quardranti-

of the plane namely XOY, YOX', X'OY'
and Y'OX respectively coilled first,
2nd, 3rd and 4th quardrant of the
plane subdivided by the coordinate
axes of the plane. They are denoted
by Q-I. Q-II,Q-IIQ-IV respectively.

Example:-

Rana Mujeeb 0303-6098695

《文文版》《《本文》

	×		-1	0
l	ď	3	3	0

Instructor Rana Mujeeb 0303-6098695

Rana Mujeeb 0303-6098695

Table .-

×	1	-1	0
7	-2	2	0

x-3m+1=0 leste, to Rana Mujeeb 0303-0098695 Instructor Rana Mujeeb 0303-6098695 h) 3x-2g+1=c Instructor Rana Mujeeb 0303-6053695 Table -

Mark Committee and the second second second second second

Instructor
Rana Mujeeb

303-6098695

3- Are the following lines is parallel to x-axis @ parallel to

i) 2 x-1=3

Rana Mujeeb 0303-6098695

1. = 2

Trus line is paralei to y-alis

11) 7/12=1

x = 1-2

x = -1

. 5 1.15

Rana Mujeeb

is parallel

to Hours.

```
(1) 2 y+3=2
              Instructor
              Rana Mujeeb
              0303-6058695
   In. I re is
                   posa"el to xaxs.
iv) 1/4 4 = 0
    This line is norther penaller to x-axis and
         nos parallell to y-cixis.
 V) 2x-24=0
   2 x = 24
    Rana Mujeeb
              0303-6098695
    7 =·4
  This line is neither parallel to x-cixis,
  and - not possilled to y axis.
  4- Find the value of m and
   c of the following lines by
  expressing them in the form wimxic.
  a) 2x+3y-1=0
                  Let.
                      y= mxt.(_____)
                   Nows
   Instructor
                        2x+3y-1=0
   Rana Mujeeb-
   0303-6098695
                        -3y = 1-2x
```

- 4= 1-2 x

-- - 2 and (. メーシャニーン ומנבעינפים Rana Mujeeb. 0303-6098695 c) 3x + 6- . = 2 Instructor Rana Mujeeb 0303-6098695

1+6 xx C - , _

Instructor

Rana Mujeeb 0303-6058695

Nows

Rana Mujeeb

0303-6098635

f) 2 x ± 4 + 3

21.3

Instructor Done 11

د ي ک ک ب

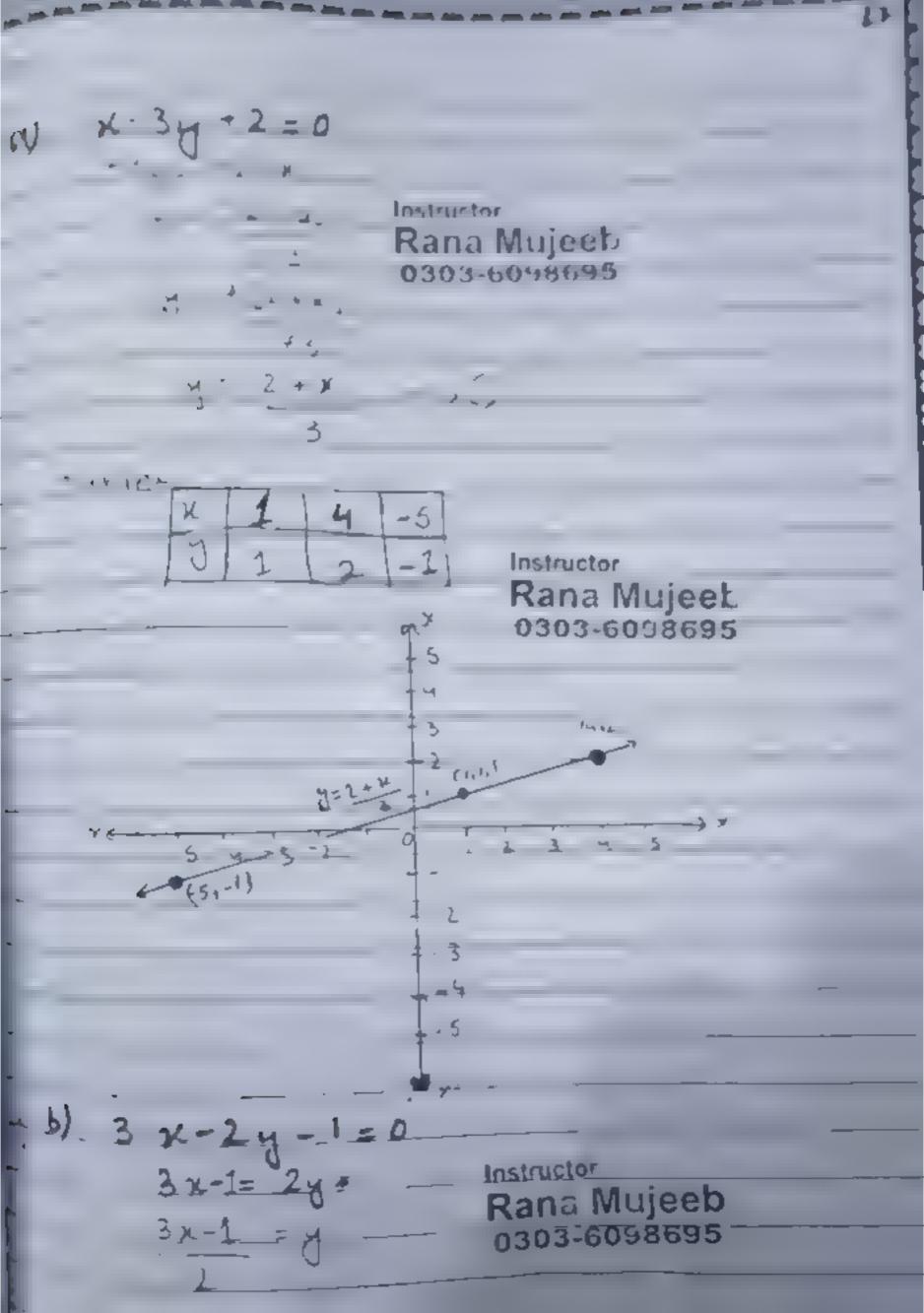
Rana Mujeet 0303-6098695

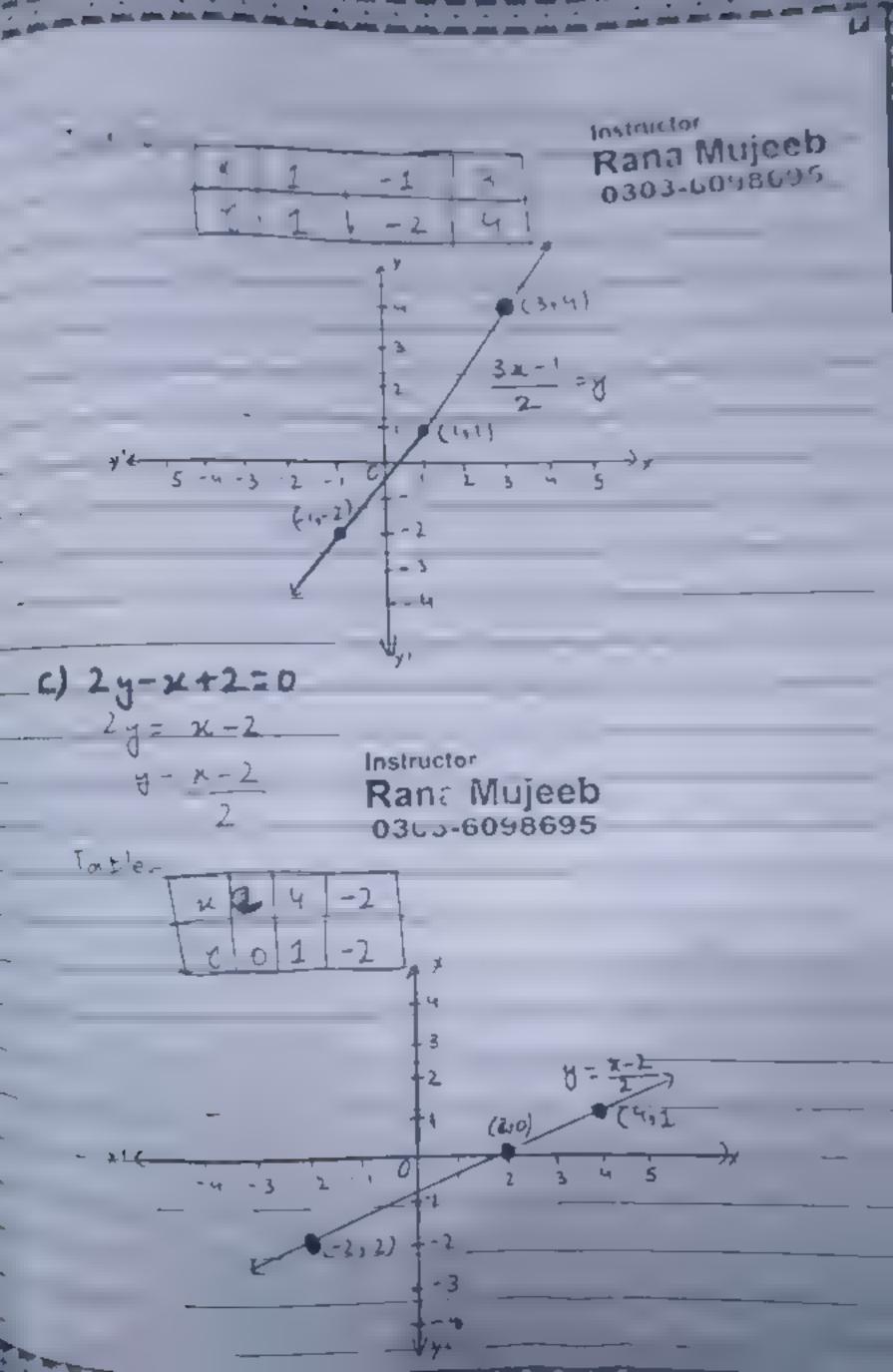
11-2 35=-5.

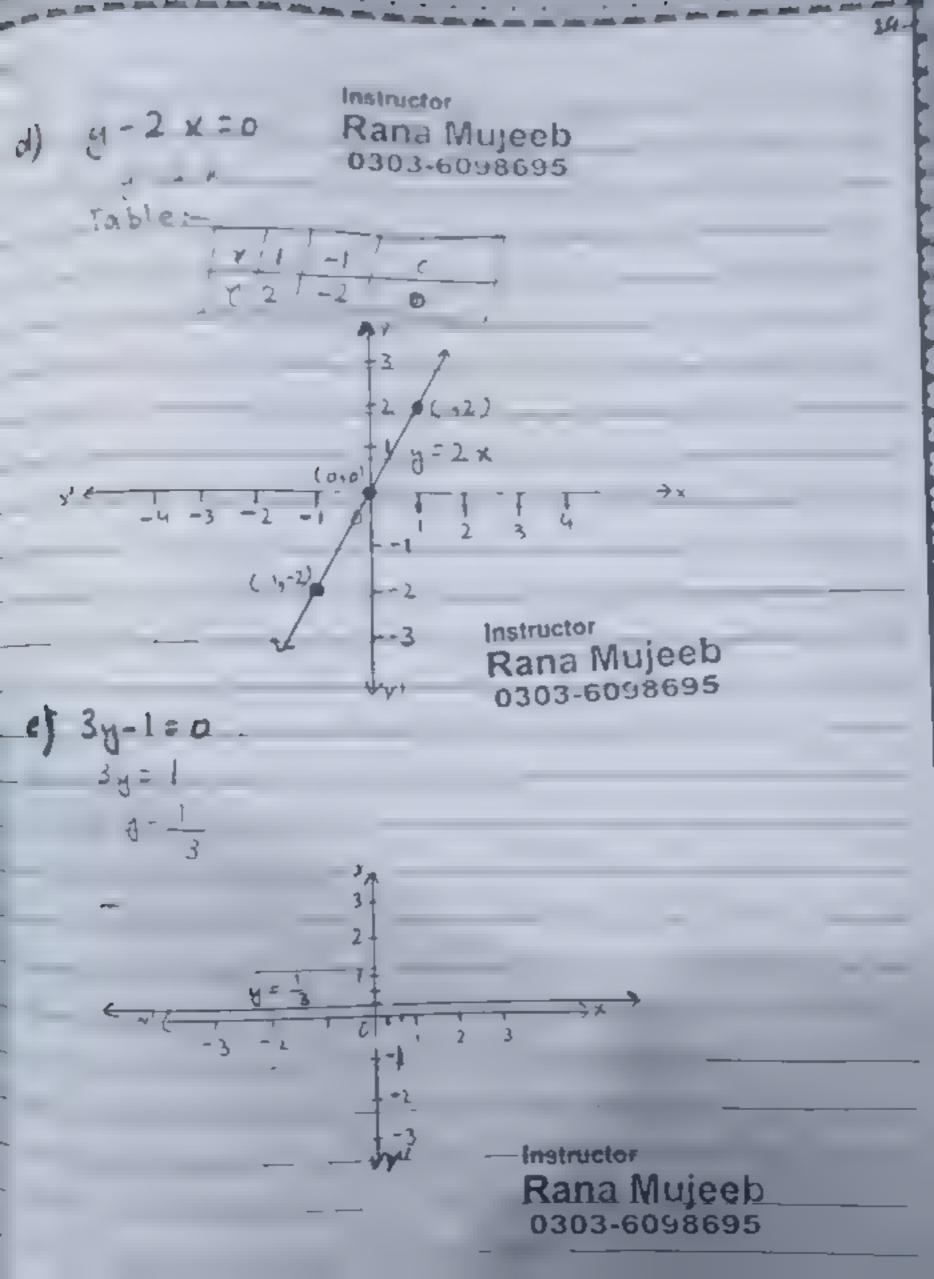
```
5 - serify whether the following
 point lies on the line
   2x-y+120 or not.
 i) (2,3)
   Lets_
   2 - 2 - 0
     14 34 ~ L Instructor
    1 + 1 - 5 Rana Mujeeb
     2 # L 0303-6098695
    The paint dos not is on
       tre ire
  ii) (0,0)
   et,
      Dr 50 + 4-12
   (sat Cons. r 62, Co Instructor
                     Rana Mujeeb
   216,-6 = ===
                     0303-6098695
  The part declare we co the
- Jii) (-1,1)
 _ p+,
            21-2+1=2-15
         Fit (= 1 - 12 - 2)
           2(-1) + 1 + 1 = 5.
```

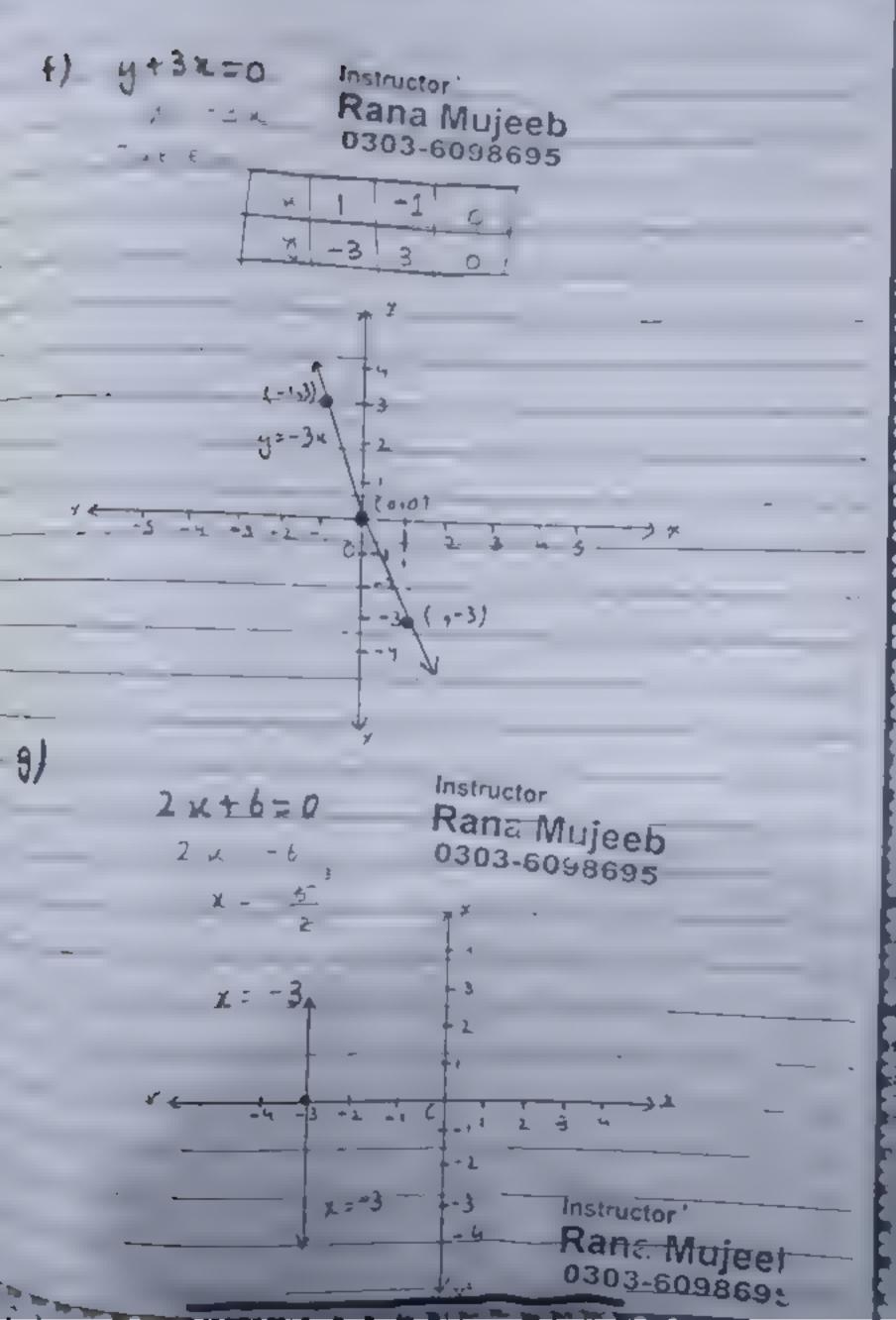
4

```
Instructor
                    Rana Mujeet
                    0303-6098695
        1 15
    iv) (2,5)
     Letz
         2x-4+1=0-12
     Pat (2,5) in ea 2:
        2(2)-5+1=0
         14-5+1= E
                      Instructor
           Rana Mujeet
              0 = 0 0303-6098695
    The point lie on the line
   V) (5,3)
          Leti
              2 x=4+1=0 ->2
          Fut [5,3] .x. eq. 0
             2(5)-3 +1=0 Instructor
             10 -3+1=0 - Rana Mujeeb
                       0303-6058695
                8#5
      The point does not
            in the line.
                FX: 8.2
sisketch the graph on graph paper
      of the following.
```









```
1) Conversion .-
                         to to tar
   a) km to mile /m le to km .- Rana Mijeeb
                           030 + 60 98695
     Imile - 1 6 km
   b) hastare to Acre/Acre to Hastare .-
     : 1 . tare 2 & egre
        12/16 - 11 - 12 DIE
   c) US Dellar to PKR :--
      1 US $ 16 46 Rapers
   d) C to F/F.C :-
         C 5 (F 32)
                      Instructor
                      Rana Mujeeb
       F- 4-C+32
                      0303-6098695
In Note: -
examples an ordered or write 1st
 simers is a and 2nd coment s & such
(xy) f (y,x) where, x 7.
 1 (2,5) and (3,2) are the different ordered
 (x,y) = (m,n) cry 1 1.m and 4:n
 Euch point pof Plane can be identified
 to Ine roudinates of the pair
  (x,y) and is represented by Plany).
 A tre prints of pione ray y-
 The he or x-axis 1.e., P(2)
    . fs cn -x-0115.
```

the . . 0303 6098695 (") FEVIEW EX 8:-1-choose the cornect options. (d) (1,1) (d) (1,1) Q: (x) - (c) , (re) (71) 13) (a)...,") (b) (le) (5(c, s) (o)(1,1) Olor 113 1 n quardrent, (a) I (b) II (d) IV Oll glutt, x 2 thin jis, (a) 2 (b) 3 (c) 1 (a) 5 Quenich endered for sutisfies the equation 4=2x? de , 2) (6) (2,1) (c) (2,2) (d)(0,1) 2-Identify the following which statement as true or false? Ite point ((c,c) is in quadrant III. False The print p(2.0). He on x-akis. True The graph of x=-2 15 of verticle line, True 0 3 3 2 15 a. horizontal line. True Foot a(-12) is in quadrant III. Folse

23*

Rana Mujeeb 0303-60 78695

3- Lime the following grown on graph

(= 3-3), (-4,6), (4, 5), (5,3)

(-6.4) FE

Rana Mujeeb 0303-6098695

Instructor
Rana Mujeeb
0303-6098695

and armed of the filter

(4, 5)

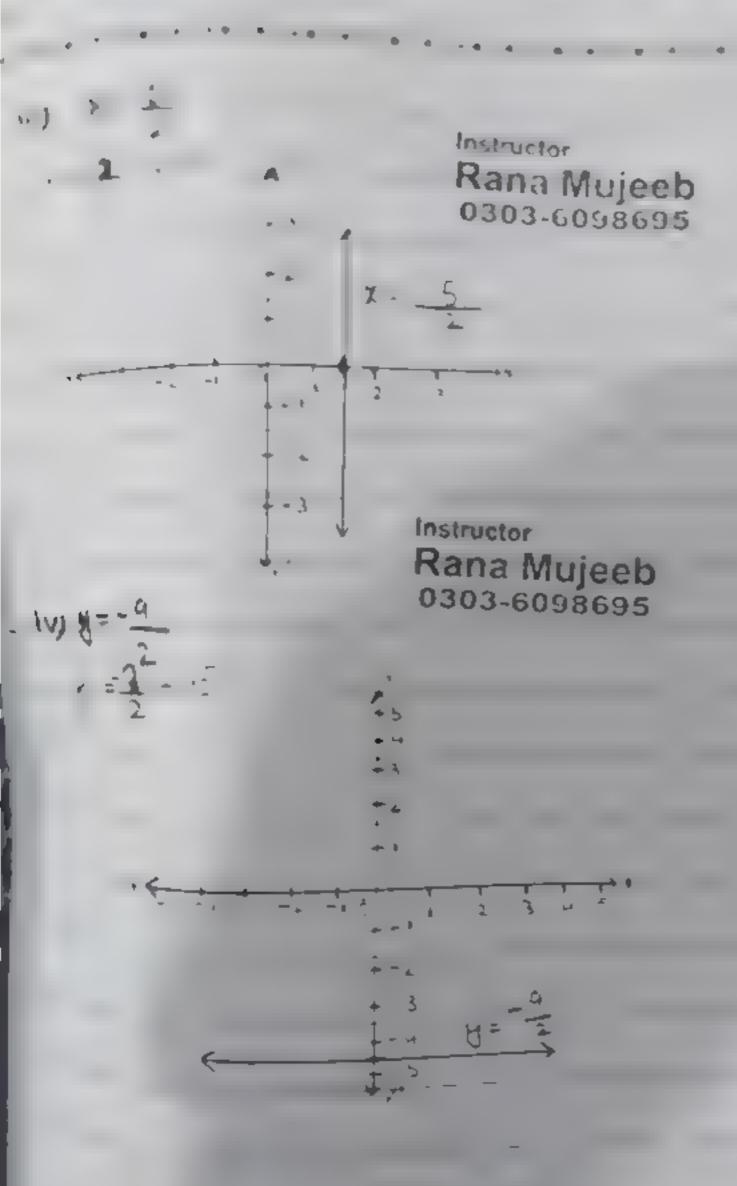
4_

Rana Mujeeb 0303-6098695

Instructor

Rana Mujeeb 0303-6098695

Rana Mujeeb 0303-6098695



Rana Mujeeb 0303-6098695 Rana Mujerb 0303-6098695

> Rana Mujeeb 0303-6098695

Rana Mujeeb 0303-6098695

× 1 -1 3 -5

Rana Mujeeb 0303-6098695

5- tran the following graph

D # 1 1 6 2 2

1 1 -1 0

(0,0)

Rana Mujeeb

Rana Mujeeb

y-062x

11) Instructor Rana Mujeeb 0303-6098695 Instructor Rana Mujeeb 0303-6098695

Chapter No 9"Introduction to

Coordinate Geometry."

Basic Concepts:

(i) Plane Geometry.

sis coordinate geometry.

collinear & non-collinear points.

Ew Triangle:

My Types of triangle.

wis Parallelogram.

(Vii) Rectangle.

Winsquare.

(ix) Distance Formula.

(x) Mid-point Formula.

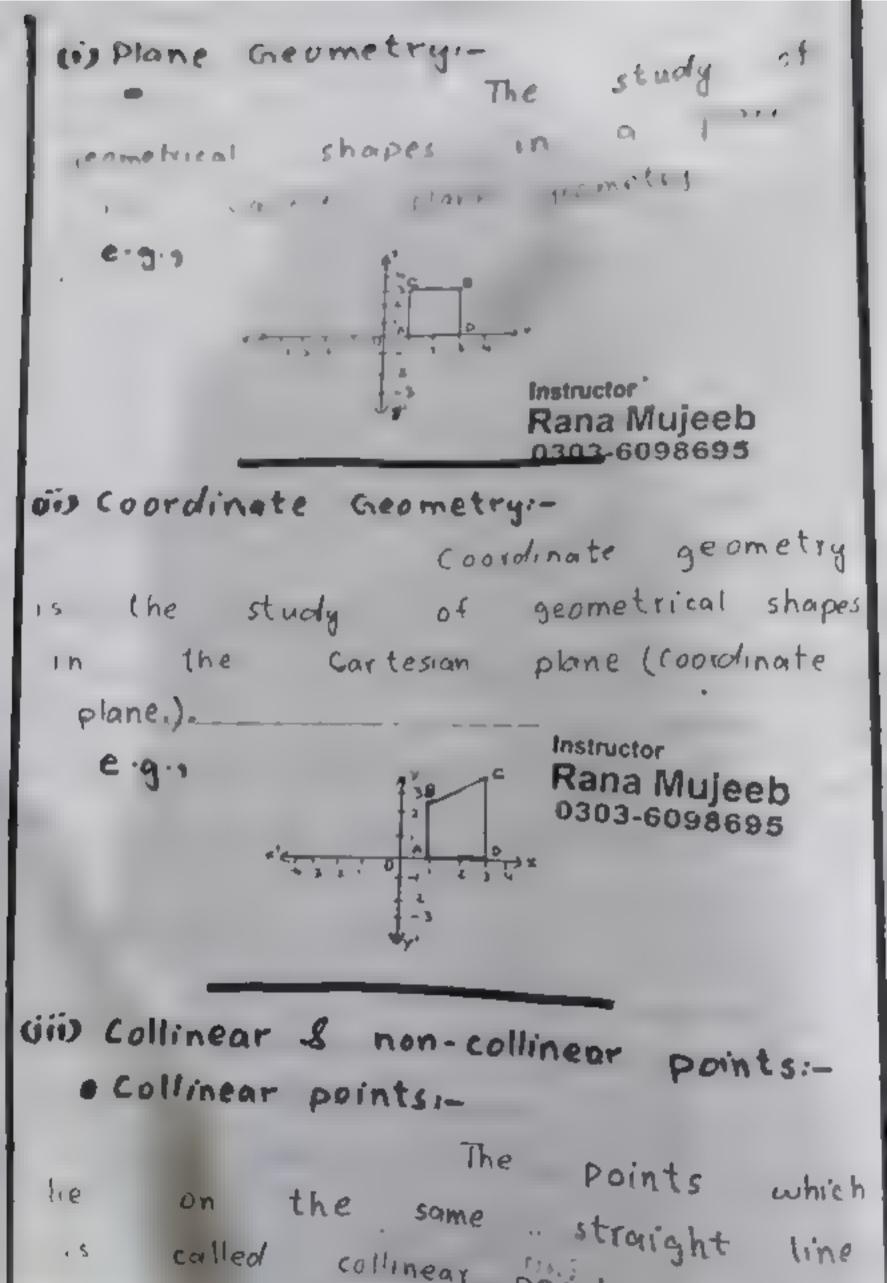
(xi) Ex 9.1.

(xii) Ex 9.2(@1,2,3,4,6,10(only))

(xiii) Ex 9.3 (Q1 (only))

criviReview Ex 9.

Rana Mujeeb 0303-6098695



called collinear points.

a Asbac one collinear prints

Non - Collinear Points:-

The points which do not le on the some straight line is called Instructor non callinear points Rana Mujeeb 0303-6098695

e . 9 . 2

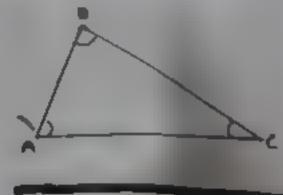
00

Here, A,B are collinear and C is non collinear.

(iv) Triangle:-

a geometrical closed having three sides and shape three angles is called triangle.





(v) Types of triangles - interes. · By Sides -Rana Mujeeb 0303-6098695 cas Equilateral triangle .-A triangle sides of equal the lta atim cand equatoral trange rength (b) I so scele triangle :triangle with soles of equal length two cated isosce p 's usage 15 6.3.7 Instructor Rana Mujeeb 0303-6098695 esscalene triangle:-A tiorae eratr different the sides of scalene triangle is co.'ed 6.8.

By Angles .posAcute angled triangle measuring less than acalled ocute mary to anse 6.99 (b) Right angled triangle a triangle with eter er brat measura on ed sur anged transfe 5 Instructor e 9" Rana Mujeeb 0303-6038695 es Obtuse angled trianglestriangle with שיבור וונשני מת שלה בים SPE thon ?: S 25 83 EE USE ANG ES Instructor e 97 & Rana Mujeeb 0303-6098695 17

(vi) Parallelogram - Rana Mujeeb

- of ... site angles use some
- The diagonals but to the

e.g.,

7 4 7

(vii) Restangle -

A figure formed in

tre pone by for non-collinear
ponts s cover testinge . f.

- # I's coposte sules one equa in length
- The arge at each vertex s of measure 90°.

e .g.,



Rana Mujeeb 0303-6098695

(viii) Square:-

fave the plane formed

by four -non-collnear pants

suir that -engine of all sives

200 18 90°.

8.90 Rana Mujeeb
0303-6096695

Gx) Distance Formula -

Ef P(x, 14,) and a cond a cond

(x) Mid - point Fermula:- 0303-6098695

If P(xiry) and Q (xxiry) and R(xxy) are two points in the plane, then the mid-point R(xxy) of the line segment PQ 15

R(x,y)= R(x1+x1, 41+y1).

the following pairs of points.

(a)
$$A(9,2)$$
, $B(7,2)$
 $|AB| - \sqrt{|x_2|} + |y_1|^2$
 $|AB| = \sqrt{(7-9)^2 + (2-2)^2}$
 $|AB| = \sqrt{(2)^2 + (6)^2}$
 $|AB| = \sqrt{4}$
 $|AB| = \sqrt{4}$
 $|AB| = \sqrt{4}$

Instructor Rana Mujeeb 0303-6098695

(W A(2,-6), 8(3,-6)

$$|AB| = \int |x_2 \cdot x_1|^2 + |y_1 - y_1|^2$$

 $|AB| = \int (3-2)^2 + (-6-(-6))^2$
 $|AB| = \int (1)^2 + (-6+16)^2$
 $|AB| = \int (1+(0)^2)$
 $|AB$

(C) A (-8.1), B(6.1). $(AB) = \sqrt{(x_2 - x_1|^2 + |y_2 - y_1|^2 + |y_2 - y_1|^2 + |y_2 - y_1|^2 + |y_2 - y_1|^2}$ $|AB| = \sqrt{(6 - (-8))^2 + (1 - 1)^2}$ $|AB| = \sqrt{(6 + 8)^2 + (6)^2}$ | AB| = AU4)*

Instructor Rana Mujeeb 0303-6098695

(a)
$$A(-4.\sqrt{2})$$
, $B(-4.-3)$
 $|AB| = \sqrt{|x_1|^2 + |y_1 - y_1|^2}$
 $|AB| = \sqrt{(-4-(-4))^2 + (-3-\sqrt{2})^2}$
 $|AB| = \sqrt{(-4+4)^2 + (-3-\sqrt{2})^2}$
 $|AB| = \sqrt{(0)^2 + (-3-\sqrt{2})^2}$
 $|AB| = \sqrt{(-3-\sqrt{2})^2}$
 $|AB| = \sqrt{(-3-\sqrt{2})^2}$
 $|AB| = \sqrt{(-1)^2(3+\sqrt{2})^2}$
 $|AB| = \sqrt{(-1)^2(3+\sqrt{2})^2}$

IABI = 3+12 Instructor

Instructor
Rana Mujeeb
0303-6098695 ---

(c) A(3,-11), B(3,-4) $|AB| = \lambda |x_2-x_1|^2 + |y_2-y_1|^2$ $|AB| = \lambda (3-3)^2 + (-4-(-11))^2$ $|AB| = \lambda (0)^2 + (-4+11)^2$ $|AB| = \lambda (7)^2$ $|AB| = \lambda (7)^2$ |AB| = 7

(f) A(c, c), b(c, 5)

0 01000---

ABI = 16 ...

ABI = 102 + 6-51

IABI = 125

IABI = 125

2:- Let P be the point on x-axis with x-component a and Q be the point on y-axis with y-coordinat b as given below. Find the distance blu P and Q.

(i) a = 9, b = 7Rana Mujeeb
0303-6098695

-

-

 $d = \int \frac{1}{12} \frac{(9,0)}{12} \cdot \frac{(9,7)}{12}$ $d = \int \frac{(9)^{2} + (7-0)^{2}}{(7-0)^{2}}$ $d = \int \frac{(9)^{2} + (7)^{2}}{(7-0)^{2}}$ $d = \int \frac{(9)^{2} + (7)^{2}}{(7-0)^{2}}$

pin ot = 2 , b = 3 Rana Mujeeh

1101.

1 15 (2 10) 5 Q 15 (C, 3)

d [(0.2) = (3.81)

d [(-2) = (3)

d [(-2) = (3)

00 a= -8, b= 6

Here, __

P 15(-8,0), Q is(0,6)

d= 1 [22-212+18,-412 d= 1 (0-(-8))2+(6-0)2

d = 1(0+8)2 = (6)2

d= 1(8)2+36 _

d= 164+30

d = 1100-

Instructor
Rana Mujeeb
0303-6098695

LIW a= -2 = b==3_

Pis (-220) 2 Q 15 (01-3)

- d = [(2 x1]2 + 14. 412 d = [(0-(-2)]2 + (-3-0)2

راء بالبوه d = [13] Instructor Rana Mujeeb 0303-6098695 m a= 12, b=1 Here . P 13 (12,0) , (1,12) 1 - 1 | 1 x x 1 2 + 18 8 12 d-1(0-82)2+11 c12 d= 1(-12)2+(1)2 d= 12+1 d= 13

Rana Mujeeb
0303-6098695

Here,

$$P = \frac{15}{5} (-9.0), Q = \frac{15}{5} (0, -4)$$

$$d = \frac{12x - 41^2 + 18x - 81^2}{4 \cdot 4(0 - (-9))^2 + (-4 - 0)^2}$$

$$d = \frac{12x - 41^2 + 16}{4 \cdot 4(0 + 9)^2 + 16}$$

$$d = \frac{12x - 41^2 + 16}{4 \cdot 4(0 + 9)^2 + 16}$$

$$d = \frac{12x - 41^2 + 16}{4 \cdot 4(0 + 9)^2 + 16}$$

```
ומיניווינים ו
              Rana Majeeb
             030+4, 110,45
3----
1401 2 | | No - 21 2 7 1 2
ABI . . .
E. 1 2 42 4. " = 62 3 .
186 - 2 (-2 -, - 60-2.
1 CAL A . AL AL - 45. 15
1CA, 1(1(2,, +(30,
According to profesages these
  (Hop) = (B+>c) + (Frent
  Nows
  [AB] = 10.
                 Instructor
    1BC1 = 52
                 Rana Mujeeb
     KAT - 18
                 0303-6098695
 Hence .
     Q 10+13 + 52
     @ 10,52 ± 18
    @ 18+52 # 10_
 So, it is not a right anger
          triangle-
41- Here,
       A is (4210) 2 Bes (221) 2 C 15 - 23-3-
1AB1= 1/2-21/2 1/42-4/4
LABI= (1-4)+ (1-10) = 19+81 = 11
18C1 = [ [42-x1] + 182=8-1
```

4 -2 +(+ 1 . 4 ++1 - dag A. A Mart 12 4 As W (A) _ 4-(-2), +(0-(-8), 1 , 36+324 - 6360 A 5 .

> 1AB1 + |BC1 - (CA) 190 + 190 - 1300 29 x0 + 29 x0 = 236×10 3/10 + 3/10 = 6/10 6 Sto = 6 No

So, the points A, B, C are collinear

Instructor

Rana Mujeeb

0303-6098695

6:- Heres

As,

C 15(-2,15), A 15(0,7), B 15(3,-5) 1CA1 = 1(0-(-2))2+(7-15) = 14+64 = 168 1AB)= [| 12 - 21] + | 12 - 212 1ABL=1(3-0)2+(-5-7)2 = 19+144 = 153 16 Bl= / 142-4112+ 182-4.12 1CB= (3 (-2)) + (-5-15) - 25+ 400 = 25

1CAL + [AB] = 1CB] 162 +1153 = 1425 0303-6098695 24×17 + 29×17 = 525×17 2 517 + 3 517 = 5517

Instructor Rana Mujeeb So, the yours 18,8,0 mes Whinear

10 - Here,

C(5.6)

16-

P(1,3)

Will Ex 9.3:-1:- Find the mid-point of the line segment joining each of the following pairs of points-

Mid-point of
$$AB = \begin{pmatrix} x_1 + x_2 \\ 2 \end{pmatrix}$$
Instructor

Instructor

Rana Mujeeb 0303-6098695

and point of AB

(8, 2)

Mid point of AB = (2 5 . - 6)

$$\frac{1}{2} \left(\frac{2}{8 \cdot 6}, \frac{1 \cdot 1}{2} \right)$$

Mid-point of AB = (-1,1)

Rana Mujeeb

(d) A(-4.9), B(-41-3)

Mid-paint of AB -
$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{-2}\right)$$

M1 . 1 pr. 11 04 18 (13 3)

(e) A(3,-11), B(3,-4) Mindpoint of AB - (* 1+ +2 > 0.14) (3+3 , -11+(-4)) " " = (5 , 11 + 4) " (3, -15)

Mid point of AB - (3, 75)

Instructor

(f) A(0,0) B(0,-5) Rana Mujeeb Mid-painte of AB = (with , bitts

" = (010 > 0+(-5))

" " (-) , 2-5)

11 12 11 = (09 - 5)

Mid-point of AB = (0, -25)

030 3-609нвля LXIV) Review Ex 91-1:- Choose the correct answers (i) Distance E/w points(0,0) and(1,1) 14 (6)2 (6)2 (6)2 To Distance b/w & points (2.0) and (oil) is; (NO (b) 2 (d) 2 Mid-point of points (2,2) and (0,0) is; (1,1) (W(1,0) (c)(0,1) (d)(-1,-1) in Mid point of points (2,-2) and (-2,2) is i (a) (2,2) (b) (-2,-2) (a) (0,0) (d) (2,1) (A triangle having all sides equal is __ called ; (b) Scalene (WI soscele (d) None of these @ Equilateral (Vi) A. triangle having all sides different i's called; (a) I so seele ____ 6 Scalence (C) Equilateral 60 None of these. 22 Answer - the following , which is true and which is false. in A line hors two end points. False - sua line segment has one end point. Folse triangle is formed from three ... collinear points. False

20dust a size of it to make the se c rest set to True to the ted presents of each sinde of in tungle aux co neur True WIAII the points that lie on the x-axis one collinear. True winderigin is the only point collinear with the points of both the arxes separately True: 31- Find the distance b/w the following pairs of points. (b,3),(3,-3) Instructor
Rana Mujeeb
0303-6098695 Let,

Rana Mujeeb
Let,
0303-6098695

A is (6,3), B is (3,-3)[AB] = $\lambda (3-6)^2 + (-3)^2$ [AB] = $\lambda (3-6)^2 + (-6)^2$ LAB] = $\lambda (3+3)$ [AB] = $\lambda (3+3)$

(H) (7.5), (1.-1) Instructor
Rana Mujeeb
0303-6098695

A is (7.5), B is (1.-1)

[AB] = [|x_1-x_1|^2 + |x_2-x_1|^2]

(ii) (0,0),(-4,-3)

Let,

Instructor Rana Mujeeb 0303-6098695

A 15 (6,0), B 15 (4,-3) 1AB1- 1/x2 x112+102 812 LABI - L-4-012+ (3-012 (AB) = 1 (-4) + (-3) -

1AB1: 21149

1 AB1 = 25

1AB1 = 5/_

4:- Find the mid-point blu following pairs of points.

a) (6,6),(4,-2) Instructor Rana Mujeeb 0303-6098695

Leta

A. 15 (6,6) . B is (4,2)

wid - point of AB = (21+22 , 41+42

· (1 , 6 ; 2) " = (5, E) Mich peined of AB (5,2) Instructor air (-5,-7), (-1,-1) Rana Mujeeb 0303-6098695 Leta A 15 (5, 1), B 15 (7,-5) Mid point of AB. (x1+ x2 , Jit 1/2 ~ = (-5+(7) , -74(5)) $N = \left(\frac{-5.7}{2}, -\frac{7.5}{2}\right)$ -4- 11 - (-12-6) Mid point of AB = (-6,-6) (in (3, 0) 2 (0, -12) Instructor Rana Mujeeb Let, 0303-6098695 A 15(8,0), B 15 (0,-12) Mid-point of AB = (xxx2, 81+72) $u = \left(\frac{8+0}{2}, \frac{0+(-12)}{2}\right)$ ~ ** = (至, 0-12)

mid-paint of AB = (4,6)

24

Q 1:-

Rana Mujeeb

Define congruent

triangle?

Ans:

Rana Mujeeti
0303-6098695

Lucy Lucy Lister

Lucy L

LC= LF

CA = F.

A P Note



G2:-

Rana Mirjeeb

Define correspondence?

Ams:-

Alle and a second to the secon

Li. to the state of the state o

Rana Mujeeb

distructos ... Ran. Mujecb 0303-6098695 Q3:-Review Ex 10 Which of the following are true and which are false? his two end fronts _ False In a transle stacre unber 1 True Instructor Rana Mujeeb 0303-6098695 Truck ponts are and to China try to an in True paralle Lacs attrices or pent. False

QLi :-Pastulates. Instructor 5.A.S Pastulate: Rana Mujeeb 0303-6098695 of two triangles. and their included angle of one triangle " congruent to the 211-11-11-11-1 - 1 de mar 1 11 1121 mas - ME 201 mm 12. (Instructor Rana Mujeeb Pastulate:-0303-6058695

Instactor C1 4 Rana Mujeeb 0303-6078697 and angles corresponding side S.A.A Pastulatein 1 1 A 1 0303-60986 35 Pana Mujech DOD SEOF BESS

Instructor 5-5-5 Postulate .____ 0303-6008695 Ran. Muleeb In a corresponde two triangles, if three side. -1. trineale ore constront to. the corresponding three sid. other, then the two triangles ... congruent (555=555). Instructor Rana Mujeeb 0303-6098695 Pastulateir. t. Ylyingen raginalis and

Instructor Rana Mujeeb 0303-6098605 corresponding side of the othe. the triangles are congruent (H.S = H.S) Instructor Q5:- VIP M CQ'Si-Rana Mujeeb 0303-6098695 If the materials congressive the sides expense them are in congruent, Q6:- If one angle of triangle is of 30 than what is its hypotenuse? Ans:- If one angle of a right triangle is of 30°, the hypotenuse is twice as long as the side opposite to the angle.

Rana Wuleeb 0303-6098695

Chapter He 11

Parallelograms and Triungles

Basic_Concepts

i. Pelygens.

ii. Quadrilaterals.

. iii . Trapeziums.

iv. Parallelograms.

Rhom bus.

vi. Rectorngles. Rana Mujeeb

vii. Squores.

0303-6058695

viii. Review Ex. 11

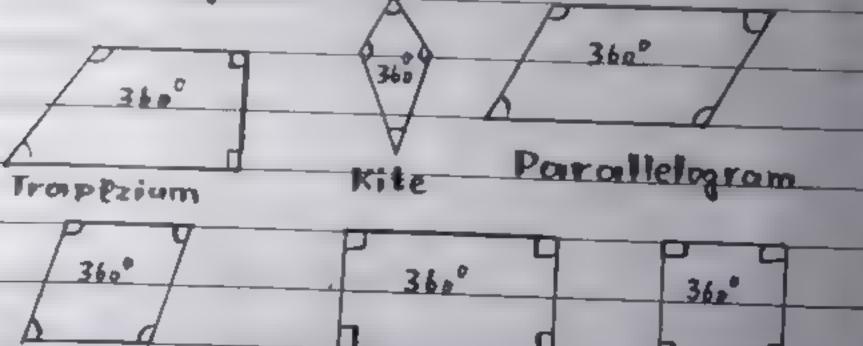
ix. Some Important Concepts.

ii. Guadrilateral: Def:

Rana Mujeeb 0303-6098695

The word quadrilateral" consist of two words one is "quadril" which means "four" and other is "lateral" which means "sides" A polygon with four sides, four angles and four vertices is called quadrilateral

Exomple:



Rhambus

Rectangle

Souware

Rana Mujeeb
0303-6098695

A P MOVES

() A 1

iii. Tropeziumi Rana Mujeeb

Instructor 0303-6098695

Def:-

is a quadrilateral with one pair of parallel sides is called trapezium:

ii) A quadrilateral with two parallel sides and two unparallell sides is called trapezium.

Examples

Trapeziums.

IV. Perrallelaram:- Instructor Def:-

A figure formed by four noncollinear points in the plane

called a paralalation 111.

DATE		
opposite sides are parallel and congruent.		
Opposite angles are congruent in) The diagonals bisect each other. Expimple:-		
Rana Mujeeb O303-6098695 Porallelegram.		
y. Rhombus:-		
Defi		
A paralleigram with all equal		
sides is colled rhombus		
Exemple: 2.6cm 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 36.7 3		

vi. Rectangles Defi

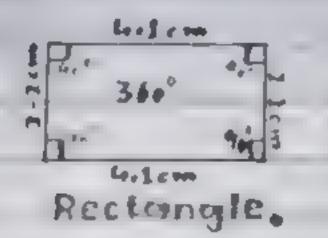
Rana Mujeeb

A figure firmed in the plane by four non-collinear points is coled rectange if.

Its apposite sides are parallel to each other.

The angle at each vertex is of measure of 90°

Excurpite:



Rana Mujeeh 0303-6098695

vii. Square:

Defi

Rana Mujeeb 0303-6098695

A square is a stoped figure in the same formed by four non-collinear points.

such that lengths of all sides are equal and measure of each ancie is and.

Example:-

triangles.

2-2cm 2-2cm 2-2cm 2-2cm	Rana Mujeeb 0303-60-3695
Soyuare.	

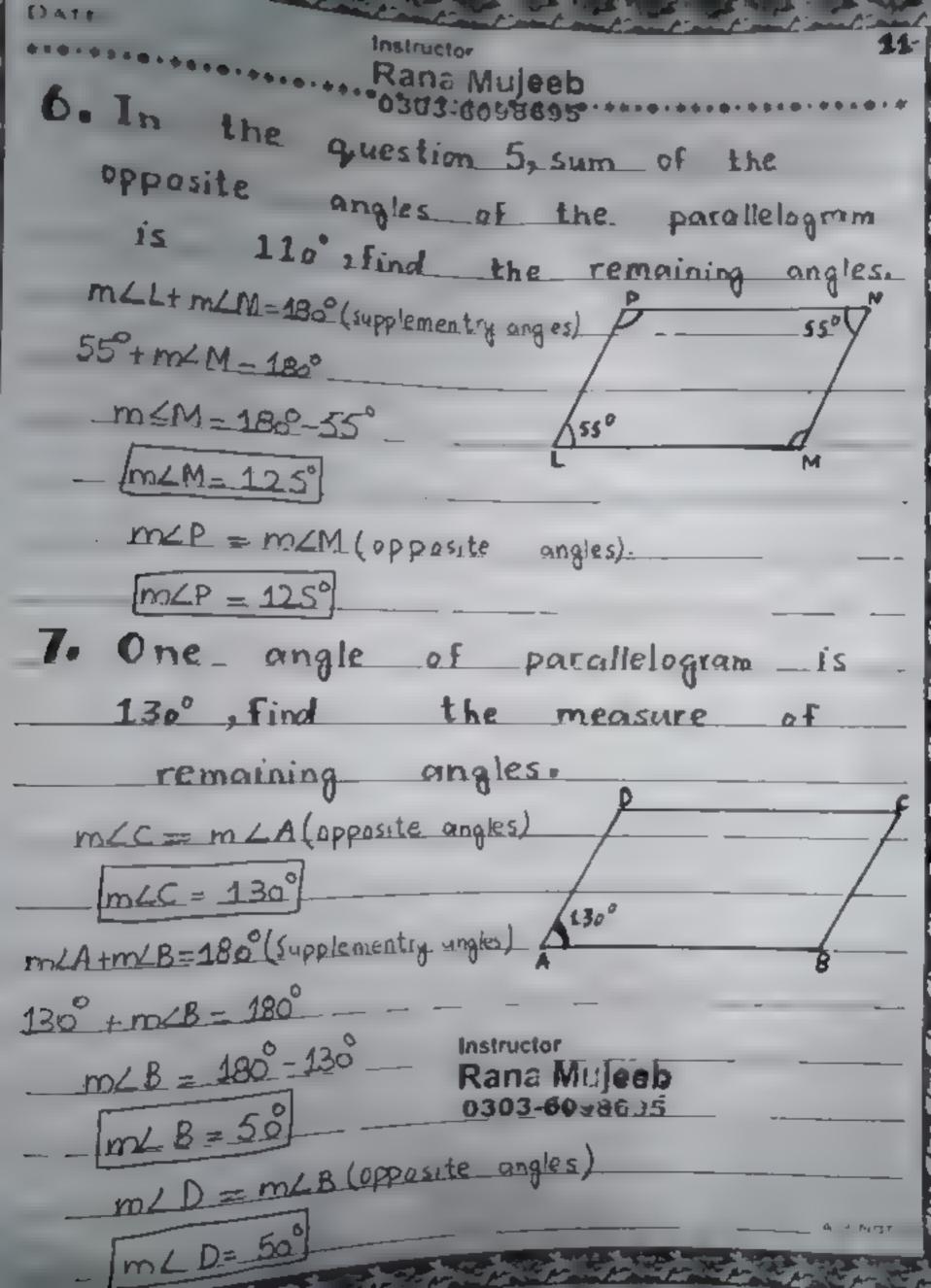
1. Fill in the blooks

- Tit in the Planks	
11 In a parallelogram opposite	sides are
i) In a parallelogram opposite	angles are
_congruent	
iii) Diagonals of a parallelogram inte	rsect each
other at a point.	
in Medians of a triangle a	re
concurrent	
v) Diagonals of a parallelograme	divides
the parallelogram into two con	

Instructor

3 O ...

4. If the given figure ABCD is a
parallelogram, then find "x, m"!-
A 52 - P(5m+10) 112 Y
mLA = m LC (opposite orgies)
55° = 11x° /55°
550 B
121
Now, Instructor Rana Mujeeb 0303-6098695
$mLA + m LD = 180^{\circ}$ (suplementry angles) $55^{\circ} + (5m + 10)^{\circ} - 180^{\circ}$
$55^{\circ} + (5m)^{\circ} + 10^{\circ} = 180^{\circ}$
65° + (5m)° = 180°
(5m) = 180°-65°
(5m)° = 115°
m° = 115° Instructor
81 Rana Mujeeb 0303-6098695
m° = 23°



8. One exterior angle on the che side of parallelegram is 40°, find 113 remaining angles. x° = 40° (Alternate angles) z° = x° (opposte angles) Z° = 40° z° +4° = 180° (Supplementry angles) 40°+40° = 180° 40= 180 - 400 Instructor Rana Mujeeb H°= 140 0303-6098695 m=40 (opposite angles) m°=140

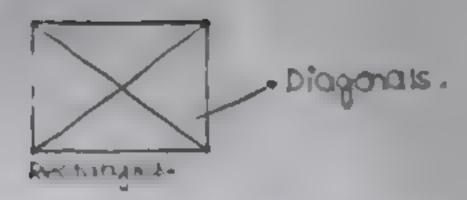
ix Some Important Concepts -

Instructor 1. Diagonals: Rana Mujeeb 0303-6098695 Defi-

A___line - segment that join two rectices of a polygon_ non-adjacent al gragonals is called

Emple

Rand Mujeeb 0303-6098695



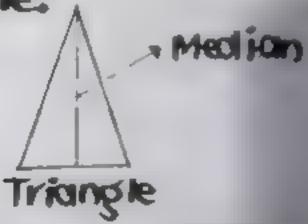
2. Mediansi

Defi-

Rana Mujeeb 0303-6098695

Median of a triangle is a majorist of opposite side.

Example:



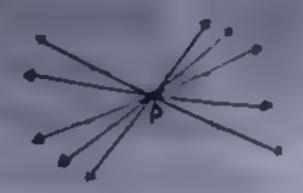
3. Concurrent:

Def:

Rana Mujeeb 0303-6098695

If a set of lines intersect each other at same

Example:



Rana Miljeeb 0303-6098695

_Here, "p" is the point

4. Theorem 11.1.2:

of a quadrilateral ore conquent

and parallel ; it is a parallelogram.

Example

Para Helogram

5. Theorem 11.1.4:

The medium of a

triangle are concurrent and

heir point of concurrency

APALI

Chapter #12-

"Line Bisectors and Angle Bisectors.

' tactor Rana Mujeeb 0303-6098695

Basic Cocepts:-

(i) Bisector of Line segment.

fijRight bisector of line segment.

(iii) Bisector of an angle.

(iv) Theorem 12.1.1.

(v) Theorem 12.1.2.

(vi) Theorem 12.1.3.

tos injetor 12:1.4. Wiis Theorem Rana Majoeb

(viii) Theorem 12.1.5 . 0 443 1 246 1505

(ix) Theorem 12.1.6.

(x) Observe that.

(xi) Note.

(xii) Theorem ...

(xiii) Parts .

Criven.

CANITO Prove

existique.

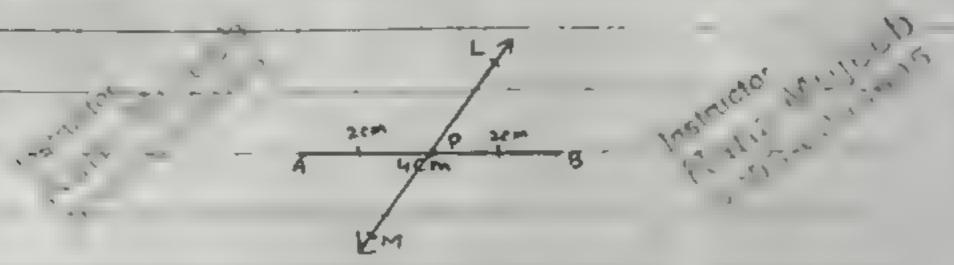
(xiv) Statement - (xxiii) Construction.

(XIX) Proof.

(200) Review Exercise 12 (Q1,2,4,5,6)

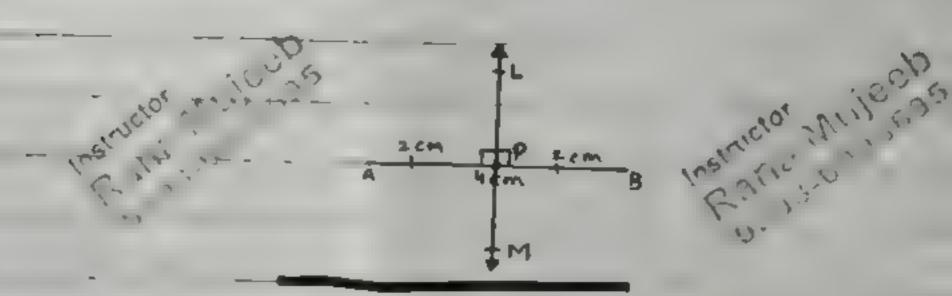
ana Muieeb

a) Bisector of Line segment: A line l is 1 called a bisector of a line segment. L passes through its mid-point.



(i) Right bisector of line segment:

A line le 15 called right bisector of line segment if l is perpendicular to the line segment and passes through its mid-point.

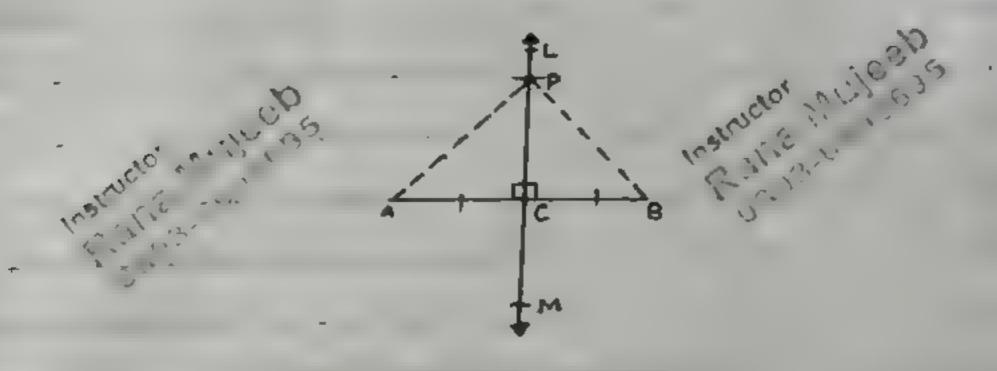


(iii) Bisector of an angler

angle is a __line or a ray that divides the given angle_into two equal parts.

_ (iv) Theorem 12.1.1:-

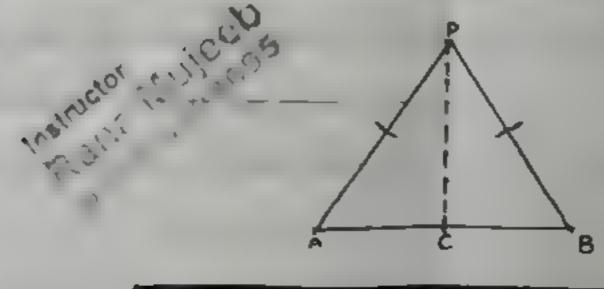
_____Any___point__on the_____
__right bisector of a line segment is equi_____distant from_its_end points.



. (v) Theorem 12-1-2:-

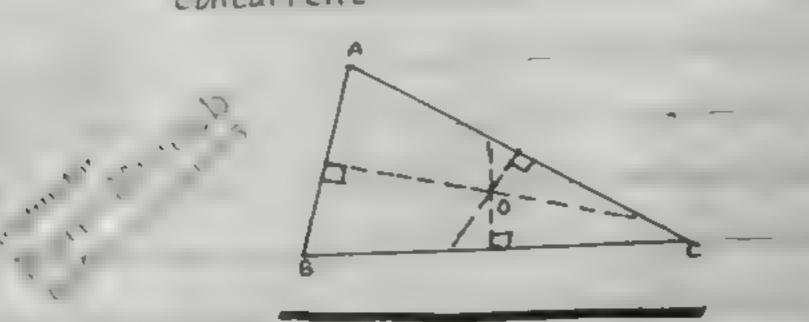
- Any point equidistant.

from the end points of a line
segment is on, the right bisector of it.



(vi) Theorem 12-1-3:-

of. the sides of a triangle are concurrent.

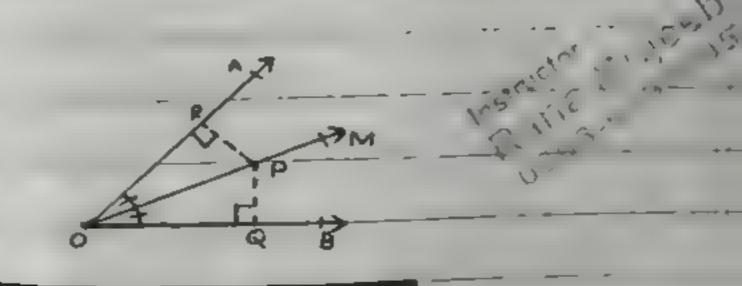


(vii) Theorem 12.1.4:

Any point on the...

bisector of an angle is equidistant...

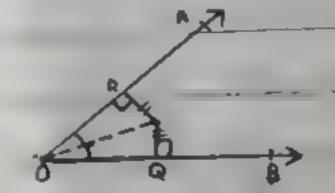
from its arms.



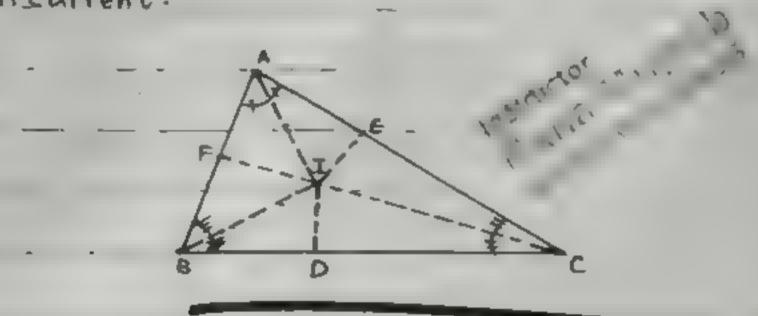
(viii) Theorem 12.1.5:-

angle, equidistant from __its_ oums, is on the bisector of it.

Instructor Mujeeb



the angles of a triangle are consurrent.



pr, Observe that:-

- The___right __bisectors of the sides
 _of__an_acute_triangle intersect each
 other inside_the triangle
- The right bisectors of the sides

 of _ a right_triangle intersect each

 other _ on _ the _hypotenuse.
- of an obtuse triangle intersect each other outside the triangle instructor

oxis Note:

by constructing angle bisectors of a triangle, we shall verify that they are concurrent.

Rana Muje

Theorem _ is a . true

statement which can be proven.

(xiii) Fourts of a Theorem:-

Costatement

(c) To Prove

(e) Construction

(b) Given

(d) Figure

(f) Proof.

Instructor Fair Mily 11,8205 11

(xiv) statement:-

The description of

a theorem in words is called

statement-

Instructor

0303-6098695

(XV) Given-

The condition described in the statement of theorem according given figure is called given. to

(xvi) To Prove:-

The required result of

Rana ' Jeeb

the theorem which is to be

proven is called to prove.

Ins' --ct--Rai W. jesh

(XVII) Figurei-A complete drawing of theorem . according given statement is called ... Instructor - ---- 4 figure Rana Mujeeb (xviii) Construction;-The additional work done on the figure in order to prove theorem is called construction. Instructor _Rana ii jeeb 0303-6098695 (xix) Proof :-The most important part of a theorem which uses statements and reasons in order to prove theorem is called proof. Rana Prije 0303-60986 (xx) Review Exercise 12:-1. Which of the following are true and which are false? (i) Bisection means to divide into _two _equal parts- True ___ Fis Right bisection of line segment means to _draw perpendicular which passes through the mid-point of line segment. True

of a line segment is not equidistant from its end points.

end points of a line segment is on
the right bisector of it. True

(**) The right bisectors of the sides of a
triangle are not concurrent. Folse

(**) The bisectors of the angles of a
triangle are concurrent. True

(**) Any point on the bisector of an angle
is not equidistant from its arms. False

(**) Any point inside an angle, equidistant
from its arms, is on the bisector
of it. True

2. If CD is right bisector of

2. If CD is right bisector of line segment AB, then:

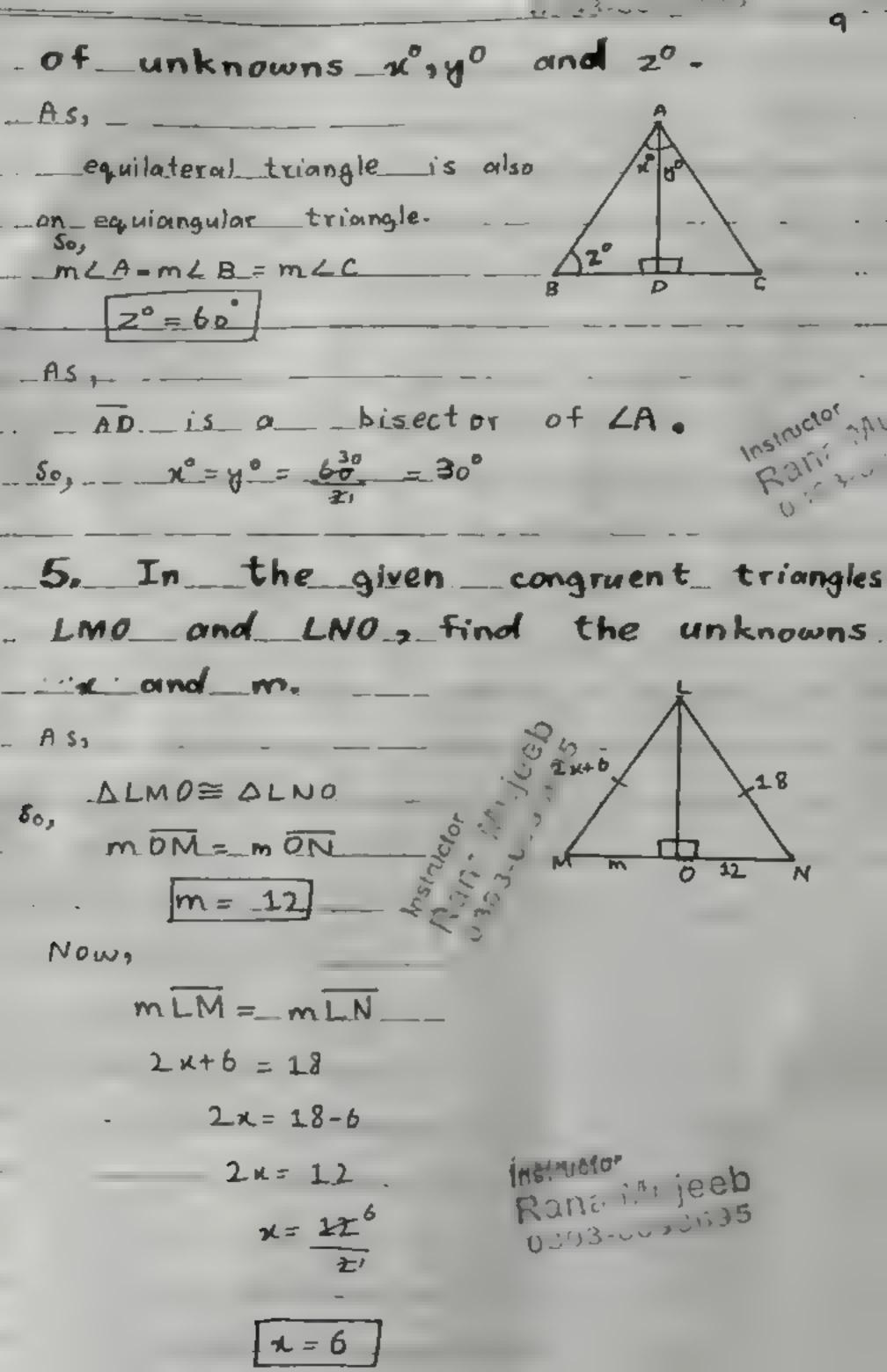
i) m OA = mOB

instructor

Rana

Ran

equilateral triangle and AD is bisector of Angle A, then find the values.



6.	CD is right	pisector _ or
the	line segment	- AB
OTF	mAB = tom, ther	find the
m	and mLB.	final_map.
(1) Lf	mBD = tiem , then	finel_ mAD.
QAs,		e
in	nAL = m LB = 63 = 3 cm	CD is
		the A SEM
	Instructor	right bisector
	Rana Mujeeti 0303-6098695	of AB.
@As,		
	$m \overline{AD} = m \overline{BD} = 4cm$	" Any print on the
		bisector of line.
	and the same of th	segment is equi-
	Lychica,	distant from
		its end points.
•		

4-4-

-

10

instructor Rana Mujeeb 0303-6098695

Chapter # 13

"Sides and Angles
of a Triagle"

Instructor

Rana Mujeeb

0303-6098695

Basic Cocepts:i) Types of Triangles.
ii) Theorem 13.1.1.

m) Theorem 13.1.2.

in Theorem 13-1-3.

v) Theorem.

vi) Theorem 13.1.4.

VII) Corollaries.

viii) Note.

ix) Review Ex. 13.

x) Some Important Cocepts.

Instructor Rana Mujeeb 0303-6098695

i) Types of Triongless. By Sides: a) Equilateral Triongle:-

the sides of equal length is called equilateral triangle.

Example:-

Instructor
Rana Mujeeb
0303-6098695

b) Isoscele Triangle:-

sides of equal length is called isoscele triangle.

Example:-

Rana Mujeeb 0303-6098695 I socele Triangle

c) Scalene triangle:-

A triangle with all the sides of different length is called scalene triangle.

Example:-



Scalene

Equilateral

Triangle

Instructor Rana Mujeeb

0303-6098695

o By Angles:- 0303-6098695

al Acute triangle / Acute-angled triangles-

triangle with all interior angles measuring less than 90° called acute triangle/acute - angled triangle.

Example:-

Acute 100 500 Triangle

b) Right triangle Right-angled triangle:-

triangle with one interior angle measuring 90° is called right triangle/ right - angled triangle.

Example:-

Right Triangle.

c)Obtuse triangle / Obtuse - angled triangle:

A triangle with one interior angle measuring greater than 90° called obtuse triangle/obtuse-angled triangle.

Example:-

Instructor Rana Mujeeb 0303-6098695

triangle. obtuse

Ran. Mujerb

iip Theorem 13-1-1:-

the two sides to the langer than the continue of the transfer than the continue of the continu



iii) Theorem 13-1-2:-

If two angles of a triangle are unequal in measure, the side opposite to the greter angle is longer than the side opposite to the smaller angle.



Rana Mujeeb 0303-6098695

iv) The oram 13-1-31-

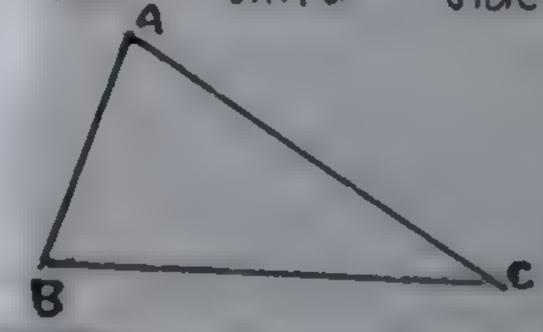
The sum of the lengths of any two sides of a triangle is greater than the length of the third side.

Conditions:-

om AB+mAC>mBC

em AB+ mBC > mAC

mBC+mAC>mAB



Rana Mujeeb 0303-6098695

VI Theorem:-

The difference of measure of two sides of a triangle is less than the measure of third side.

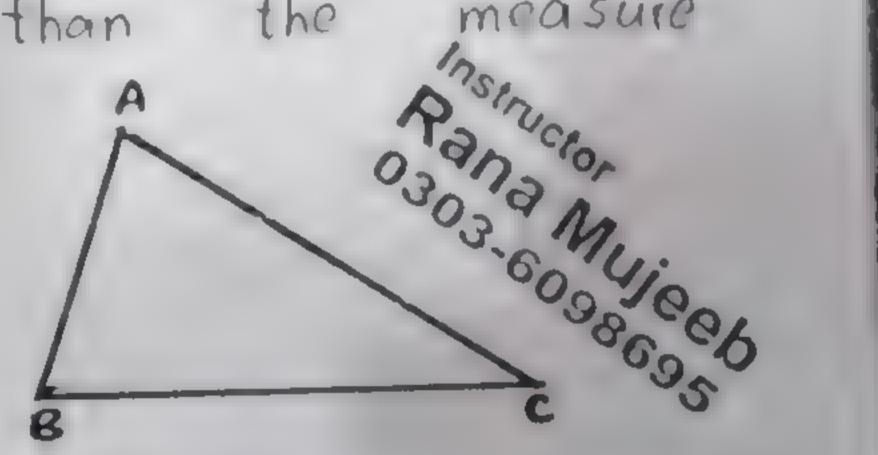
A Pansinucion

Conditions:-

MAC-MAB < MBC

MBC-MAB < MAC

MBC-MAB < MAB



vi) Theorem 13.1.4:-

From a point, outside a line, the perpendicular is the shortest distance from the point to the line.



Instructor
Rana Mujeeb
0303-6053695

vii) Corollaries:-

The hypotenuse of a right-angled triangle is longer than each of the other two sides.

In an obtuse-angled triangle, the side opposite to the obtuse angle is longer than each of the other two sides.

Rana Mujeeb 0303-6098695

viii) Note:-

on it, is the length of the perpendicular line segment from the point to the line.

The distance between a line and a point lying on it is zero.

ix) Review Ex. 13:- 0303-6098695 1. Which of the following are true and which are false?

- The angle opposite to the longer side is greater. True
- In a right-angled triangle greater angle is 60. False
- In an isosceles right-angled triangle, angles other than right angle are each of 45°. True
- A triangle having two congruent sides is called equilateral triangle. False
- A perpendicular from a point to the line is shortest distance. True
- of 90° True
- A point out side the line is collinear. False

Instructor

Instructor

Sum of two sides of triangle 1's greater than the third True 1) The distance between a line and a point on it is zero. True Triangle can be formed of lengths 2cm, 3cm and 5cm- True 2. What will be angle for shortest distance from an outside point to the line? Ans:- From a point, outside a line, the perpendicular is the shortest distance from the point to the line. Instructor Rana Mujeeb 0303-6098695

3. If 13cm, 12cm, and 5cm are the lengths of a triangle, then verify that difference of measure of omy two sides of a triangle is less than the measure of third side.

Solution:-Let,

a=13cm, b=12cm, c=5cm

Now,

0a-64C

Instructor Rana Mujeeb 0303-6098695

3

1 1 1 1 . . .

1 h- a < a

12-5= 7413

Rana Mujeeb 0303-6098695

· 0 c < b

13-5=8412

triangle is loss than the measure of third side.

lengths of a triangle, then verify that sum of measure of two sides of a triangle is greater then the third side.

Solution: - Let,

a=10cm, b=6cm, c=8cm

Now.

e atc >b

10+8=18>6

Instructor

Pho = α Rana Mujecb 0303-6098695

6+8=14>10

a+b>c 10+6=16>8

Hence proveds the sum of two sides of a triangle is greater than the measure of third side.

Rana Mujeeb 0303-6098695

5. 3cm, 4cm, and 7cm are not the lengths of the triangle. Give the reason.

Solution: Let,

a= 3cm, b= 4cm, c=7cm

Now,

• a+b>c $3+4=7 \neq 7$

b+c>a 4+7=11>3

Instructor Rana Mujeeb 0303-6098695

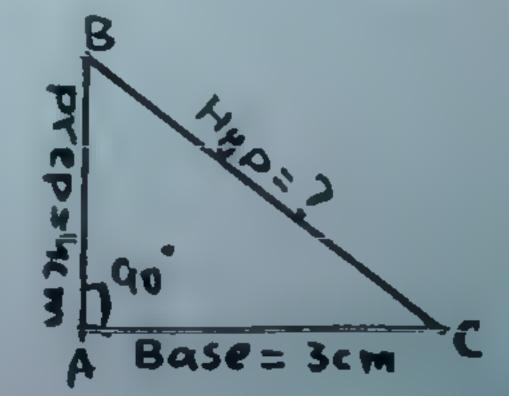
0 + c > b3+1 = 10 > 4

lengths of triangle.

6. If 3cm, 4cm are lengths of two sides of a right-angled triangle, then what should be the third length of the triangle. (Hint: Find Hypotenuse).

Solution: - According to Phythagoras theorem,

 $(Hyp)^2 = (Base)^2 + (Prep.)^2$ $(Hyp)^2 = (3)^2 + (4)^2$ $(Hyp.)^2 = 9 + 16$ $(Hyp)^2 = 25$



Rana Mujeeb 0303-6098695

By taking square root on B.S,

(Hyp.)= 125

Hyp. = 5 cm

7. Which of the following sets of lengths can be the lengths of sides of a triangle?

(a) 2cm, 3cm, 5cm

(b) 3cm, 4cm, 5cm

(c) 2 cm, 4 cm, 7 cm

Solution :-

(a) 2cm, 3cm, 5cm

Instructor Rana Mujeeb 0303-6098695

a=2cm, b=3cm, c=5cm

a+b>c2+3=5 \Rightarrow 5

0 + c > a3+6=8>2

Instructor Rana Mujeeb 2+5=7>3 0303-6098695

As, u+b >c, so, these are not lengths of a triangle.

(b) 3cm, 4cm, 5cm Let,

a=3cm, b=4cm, c=5cm

Now,

1 a+b>c 3 + 4 = 7 > 5

Instructor

Rana Mujeeb 0303-6098695

1 b+c>a

4+5=9>3

1 a+c > b

3+5=8>4

Hence proved, these are the lengths of tri angle.

(c) 2 cm, 4cm, 7cm

Let,

a=2 cm, b=4cm, c=7cm

Now,

@ a+b>c

2+4=6 \$7

Instructor

Rana Mujeeb 0303-6098695

0 b+c >a

4+7=11>2

1 c+a>b

7+2=9>4

As, a+b >c, So, these

are

not

the lengths of a

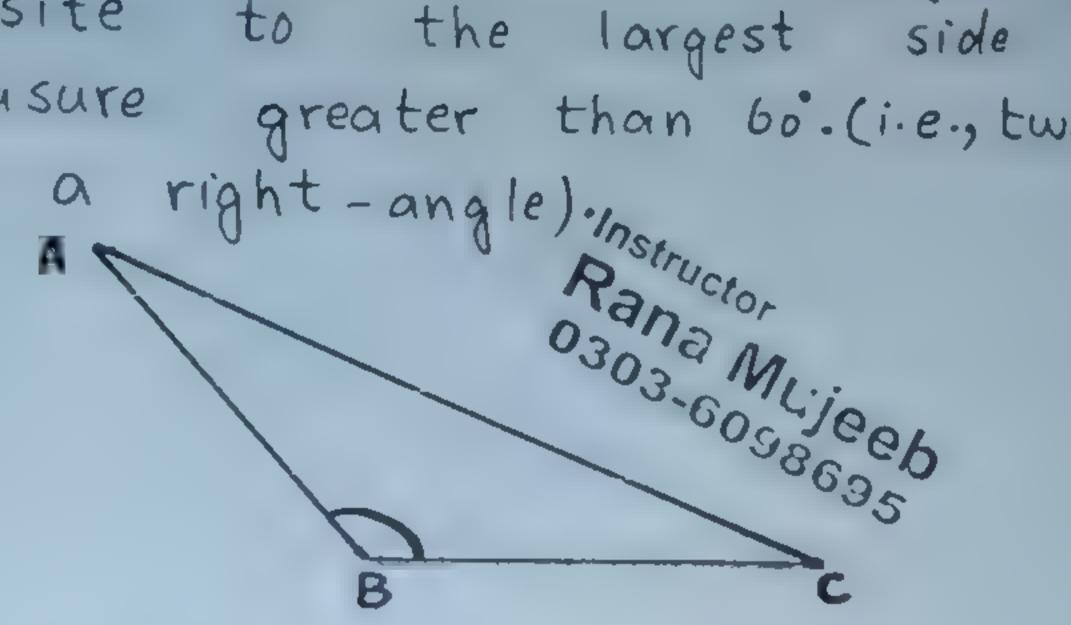
triangle-

Instructor Rana Mujeeb 0303-6098695 Instructor

Rana Mujeeb 0303-6098695

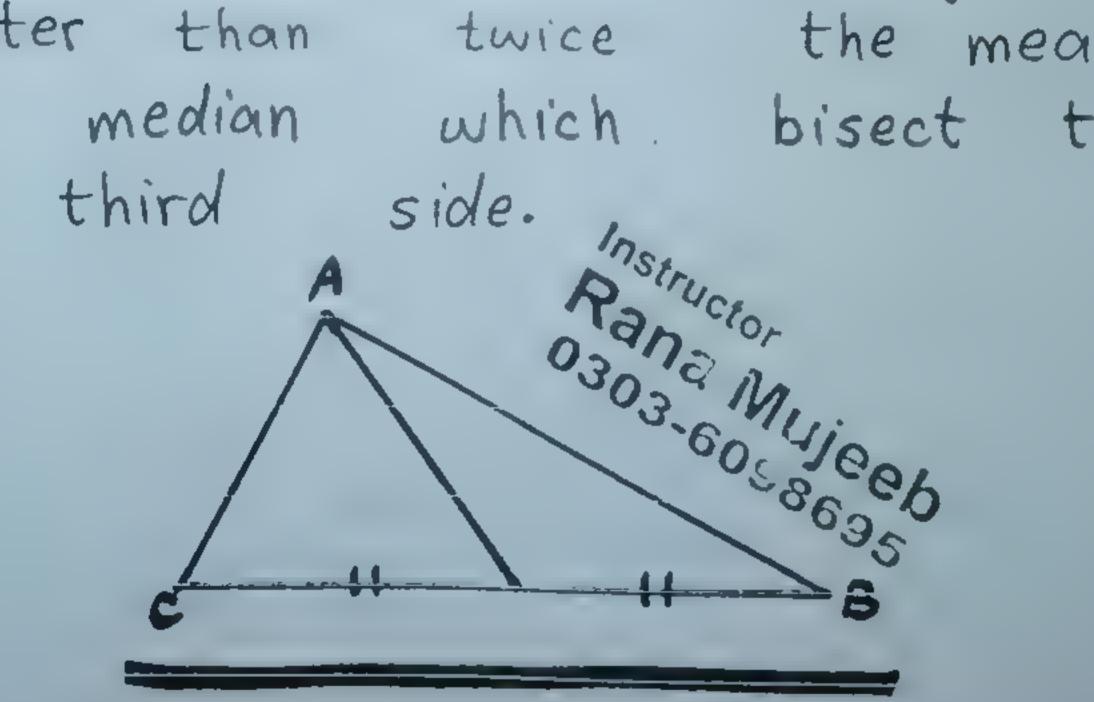
Some Important concepts: Important 1:-

In a scalene triangle, the angle opposite to the largest side is of measure greater than 60°. (i.e., two-third of a right-angle). Instru



9 Important 2:-

The sum of a measures of two sides of a triangle is greater than twice the measure of the median which bisect the third side.



Chapter #141-

Proportion

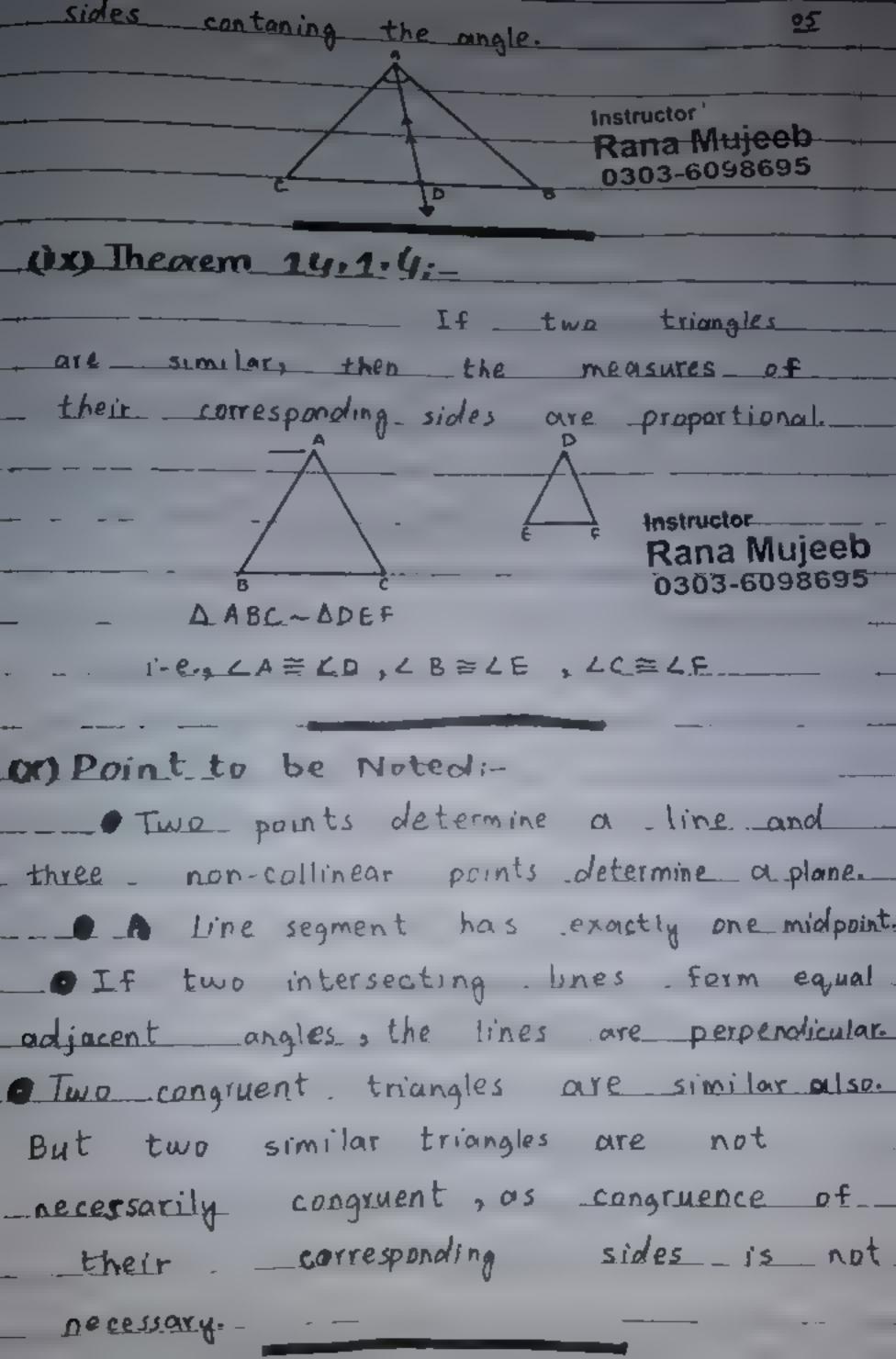
77

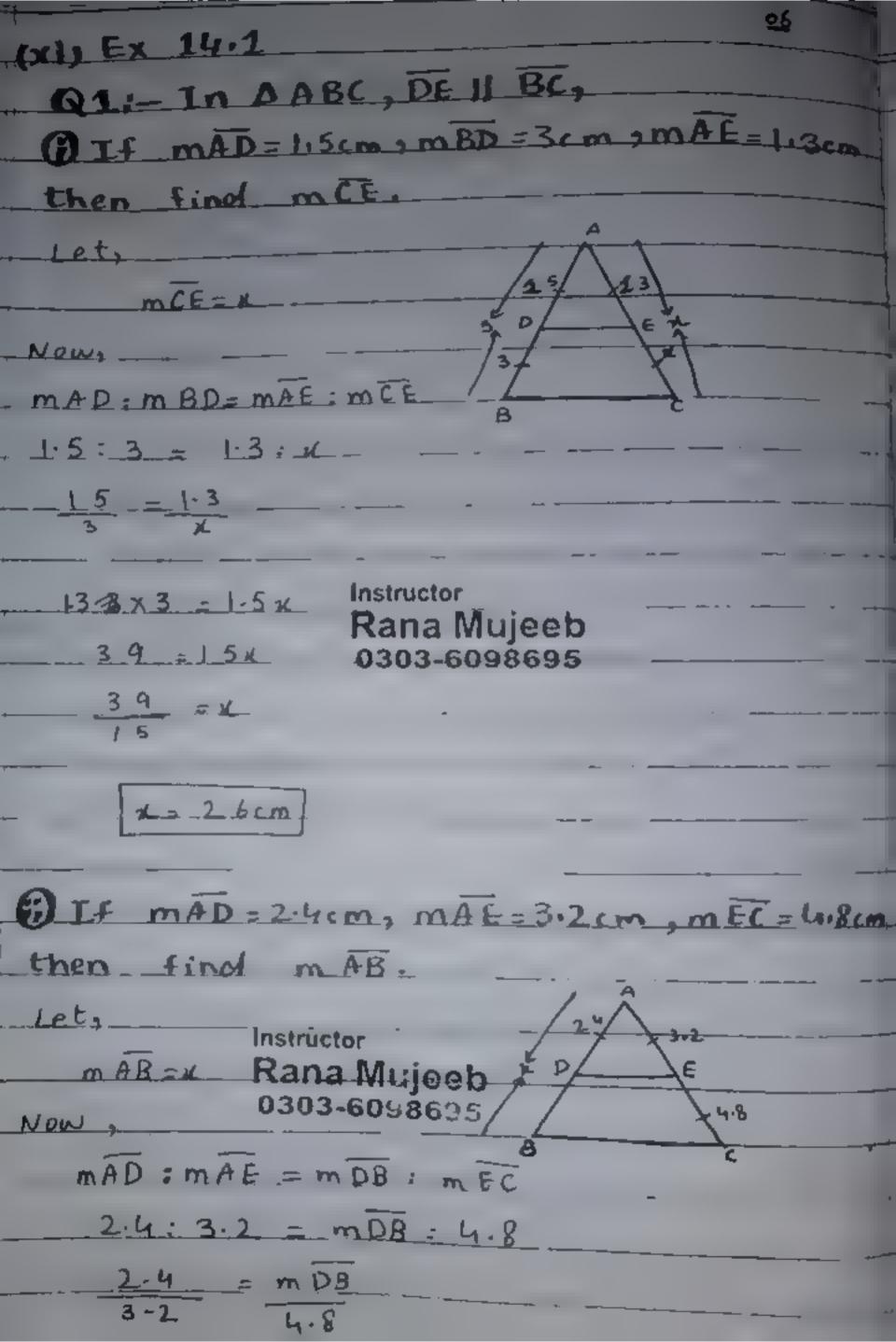
Basis_ Concepts :-_ @ Congurent triangles. (ii) Similar triangles. Instructor Rana Mujeeb (iii) Ratio. 0303-6098695 dus Proportion. of ratio wy 1st and 2nd element (vi) Theorem 14.1.1. (vii) Theorem . 14-1-2 . Instructor (viii) Theorem 14.1.3. Rana Mujeeb 0303-6098695 (JX) Theorem 141.4. (a) Point to be noted. (1) Ex142 (Q1, 1) (1) (1) (1) (1) (1) Mil Ex14.2 (Q1 & Q2 easily).

> Rana Mujeeb 0303-6098695

. pelin Review Ex 14.

(iii) Ratio:-We defined ratio a:b=a: 1. Has the __comparision of _two alike ... ; quantities a and b called the terms. i of a ratio. ... e.g., 2:3,3:5, etc. -Instructor Rana Mujeeb 0303-6098695 .. (iv) Proportion:-Equality of two ration is defined as proportion. i.e, if asb=c:d, then as b, c and .. d are said to be in proportion. e-9.7 _ 2:3 =1:4 ,etc. 1111st and 2nd element of ration-In a ratio. a:b, or is called 1st element of ratio or antecedant and bis called 2nd element of ratio or consequent. Instructor 3 -> consequent, Rana Mujee antécedant 0303-609869





2.4 x 4.8 = m BD x 3.2

11.52 = mBD x 3.2

11.52 = mBD

3.2

m BD = 3.6cm

Rana Mujeeb 0303-6098695

Sos

mAB = mAD + mDB

_ K = 24.+36

X = Bcm

IF . m AD = 35 and mAC = 4.8cm than mDB find mAE.

Let,

MAG = X

Now,

mAD:mDB = mAE: mEc

3:5 = 2 : mAC-mAE

3 = x : 4.8-x

3 = - x

Rana Mujeeb

3 (4.8-x) = 5x

14.4 - 31 = 5x

144 = 3x+5x

14.4 = 8 x

n= 14.4

M = 1.8cm |_

instructor Rana <u>Mujeeb</u>

0303-6098695

(If mAD = 2.4cm, mAE = 3.2cm, mDE

= 2cm , mBC = 5cm than find mAB.

Leta

mAB= K, m DB = y, mAC=2 , ID

m CE= m.

NOW, AADE~ AABC

> mAD = m DE = mAE MAC MAB MBC

 $\frac{2.4}{5} = \frac{2}{5}$ 3-2 Instructor Rana Mujeeb 0303-6058695

<u>08</u>

2.4 = 2. 22 5

and

2-4×5=2x and

2XZ = 32X5

12 = 24

and

22= 16.

+26 = d

and

2= 160

X=6cm

and

2 = 8cm

Helez

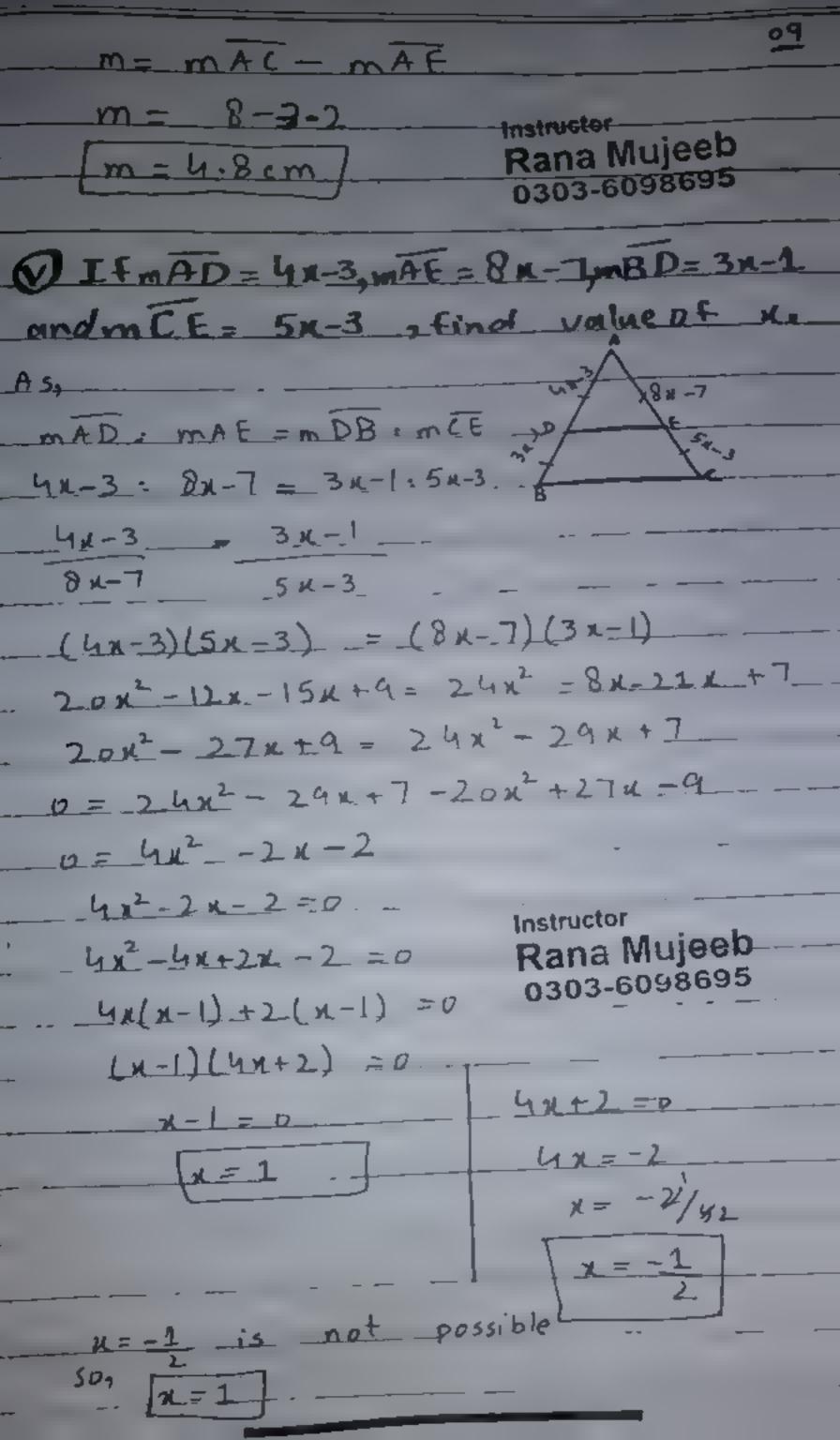
H= MAB - MAD

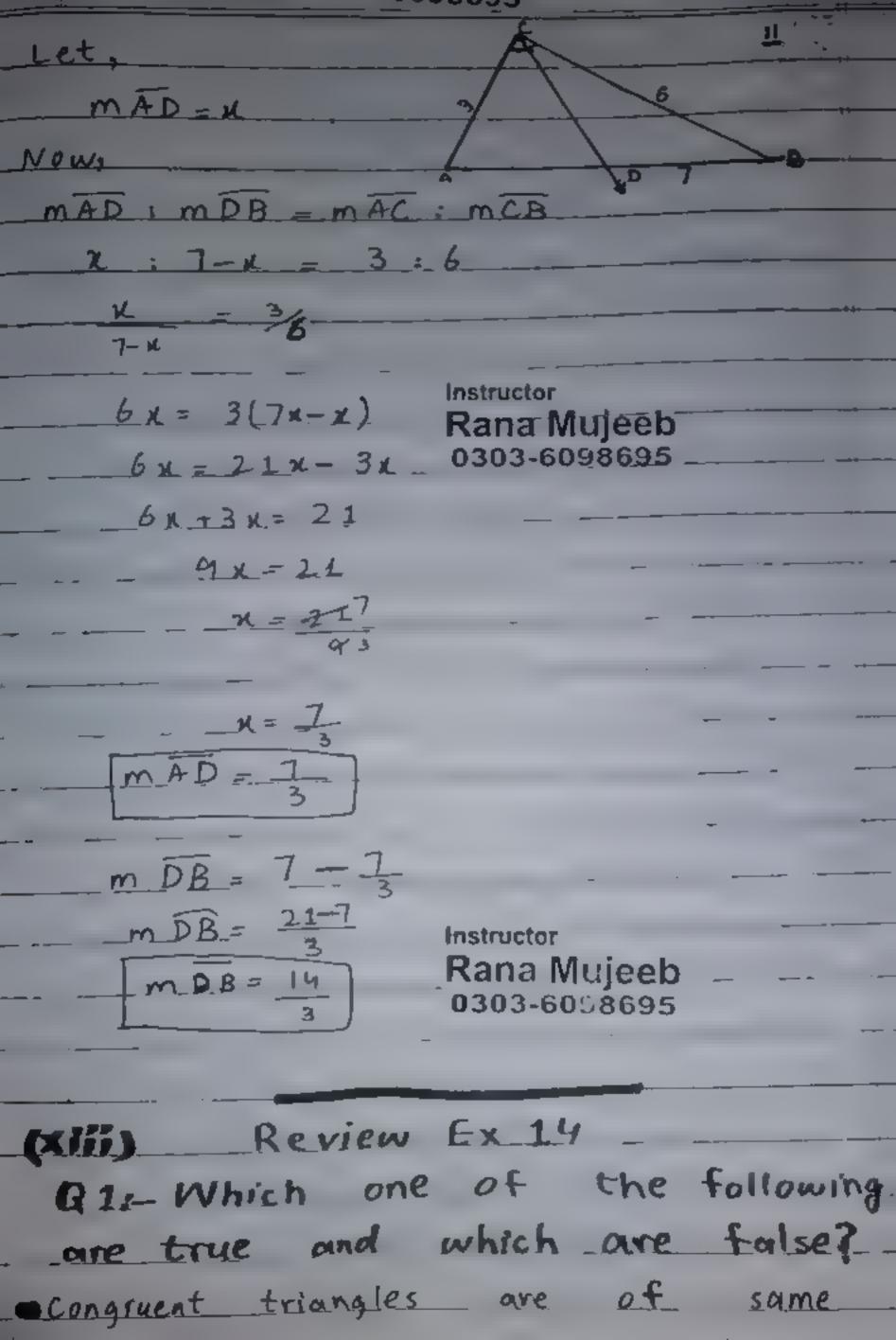
4= 6-2.4

1 = 3- bcm

Instructor

Rana Mujeeb





size and shape. True Similar triangles are of same shape but different sizes. True Symbol used for congruent is = True sybol used for Similarity is "-" True Congruent triangles are similar. True Similar triangles are congruent. False - A line segment has oney one mid-- - paint . True One and only one line can be drawn through two points. True Proportion is non-equality of two satios. False . Ratio has no unit True Q3:-In ALMIN Shown in figure MNIIPQ. 11-mLM = 5cm , mLP=2.5cm, mLQ=2.3cm then find mLN Let 1 mLN = x Nows M.LM: m LP = mLN: m LQ 5 :2:5 = *:2-3 Instructor

512.3 = 2.5x

11.5 = 2.5 x

11-5 = x

Tr=4.6cm

Instructor

Rana Mujeeb 0303-6098695

TEMEM = 6cm, m LQ = 2.5cm, m QN-5cm then find m LP. / /--

Leta

mLP = x

Noney__ = -----

mIR: mIP = m LN: m LQ

6 = x - m LQ + m QN : 25

6: x = 25+5 : 25

6 = x = 7-5 - 25

 $\frac{6}{2} = \frac{75}{2.5}$

. 6x2-5 = 7.5x

15 = 7-5 x

152 - X

1 = 2 Cm

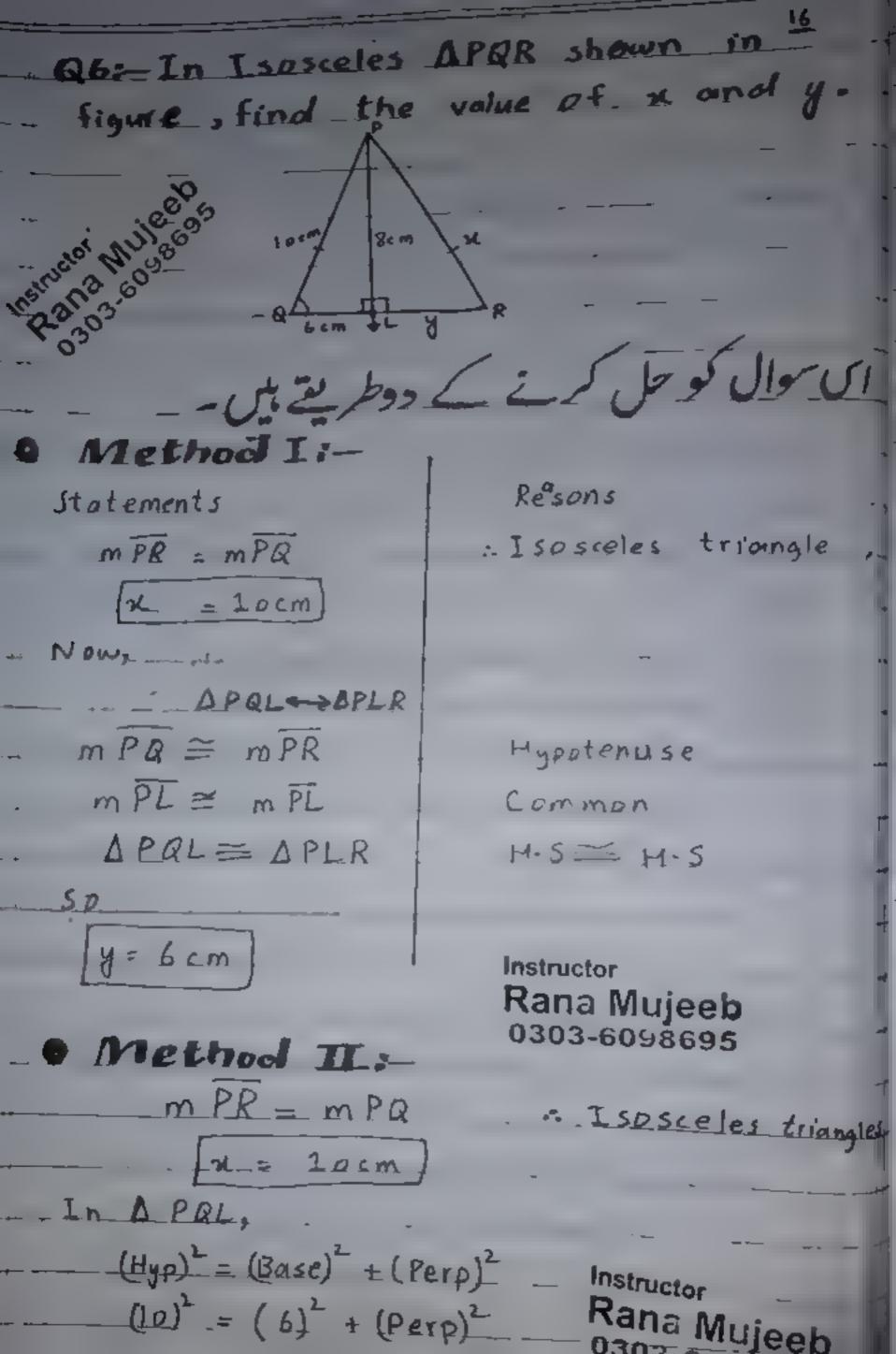
Rana Mujeeb

MPA = 8x-7, mPB = 4x-3, mAR=5x=3, mBR = 3x-1, then find value of x

if AB II QR. mPA: mPB = m AQ: mBR 8x-7 24x-3 = 5x-3:3x-1 8x-7 = 5x-3 (8x-7)(3x-1)=(4x-3)(5x-3) $24x^2 - 8x - 21x + 7 = 20x^2 - 12x - 15x + 9$ 24x2-29x+7= 20x2-27x+9 24x2-29x+7-20x2 +27x-9=0 4x2-2x-2=0 4x2-4x+2x -2 =0 Instructor 4x(x-1)+2(x-1)=0 Rana Mujee _(x-1)(4x+2)=0 0303-609869 _x-1=0 /x=1/-4x +2=0 4x=-2 x=-2/42 Instructor ' Rana Mujeeb 2 2 0303-6098695 x=-1 is not possible [x=1].

Q5= In ALMN shown in figure = LA bisects LL . If mLN=4, mLN. = b, mMN = 8, then find mMA and mAN. Let mMA = X. NOW, mMA: mAN = MML: mLN x = 8-x = 6:4 x = 6 Instructor 4x = 6(8-x) Rana Mujeeb 4x = 48 - 6x 0303-6098695 42+62 = 48 x=4.8 mMA = 4-8

$$mAN = 4.8$$
 $mAN = mMN - mMA$
 $mAN = 8 - 4.8$
 $\int mAN = 3-2$



Estructor Millogos 17 100 = 36 + (Prep)2 100-36 = (Prep)2 164 = 1(Prep)2 Prep = 8cm (Hyp)2 = (Base)2 + (Perp)2 $(10)^2 = (y)^2 + (8)^2$ A SUN WILLIAGE ST 100 = y2 + 64 100-64=42 _ 136 = 19 - | y = bcm |

Instructor'
Rana Mujeeb
0303-6098695

Chapter No 15:"Phythagoro"
theorem

Instructor'
Rana Mujeeb
0303-6098695

Basic Colepts:-

Right-angled triangle.

iii Phythagoros theorem.

iiii Converse of phythagoros theorem.

iiii Converse of phythagoros theorem.

iiii Converse of phythagoros theorem.

ivi Fx 15(01.00.02.060), 61.02

ivi Feview Exercise 15

Rana Mujeeb 0303-6098695

Instructor Mujeeb
Rana Mujeeb
0303-6098695

i) Right-angled triangle:-

one
interor angle is measuring

90° is called right-angled triangle.

e.g.,

Rana Mujeeb Rana Mujeeb

(ii) Phythagoras theorem:-

In a right-angled triangle, the square of the length of hypoteria, e is equal to the sum of the squies of the lengths of other two side.

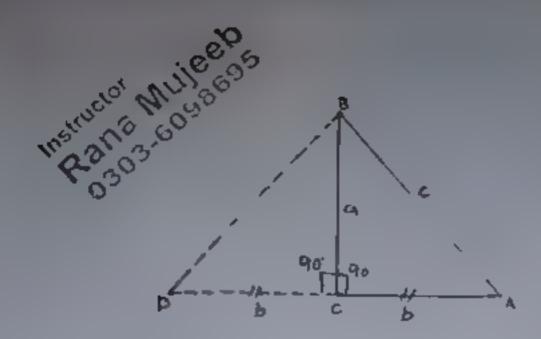
Formula:-

 $c^2 = a^2 + b^2$

Rana Mujech

ciniconverse of phythagoras theorem:—

If the square of on side of a triangle is equal to live sum of the squares of the other two sides, then the triangle is a right angled triangle.



Formular

 $a^2 + b^2 = c^2$

dw Corellary:-

Rana Mu, eb

Let "c" be the longest side "a,b and c" of a triangle.

- If a2 + b2 = c2 , then trianale is right.
- If a2 + b2 > c2, then triangle is acute.
- If a2 + b2 < c2, then triangle is obtuse.

W. Ex. 15

1 - Verify that the As having the following measures of sides are right—angled.

di a= 5cm. b= 12 cm. c= 13 cm

According to phythogens theorem, $c^2 = a^2 + b^2$ $(43)^2 = (5)^2 + (12)^2$ $169 = 25 + 144 \quad Instructor Mujeeb$

Instructor Mujeeb
Rana Mujeeb
0303-6098695

269-101

アレンド おれい マガル・ア むれい では カンドル

Hence, itisa light-angled triangle.

eu α=1.5cm, b=2cm, c=2.5cm

According to phythagoras theorem,

(25) (15)+(2)

6.25 = 2.25 + 4

6-25 = 6-25

Instructor Mujeeb
Rana Mujeeb
0303-6098695

Hence, it is a vight ungled triangle

(iii) a = 9cm , b=12cm , c= 15 cm

According to phythogoras theorem,

- - 4 + b"

15)2-(4)2+(12)2

225 = 81 + 144

225 = 225

Rana Mujeeb Rana Mujeeb 0303-6098695

Hence, it is a right-angled triungle.

in a = 16cm, b = 30cm, c = 34cm

According to phytragoras theorem,

c2 = 32 + b2

 $(34)^2 = (16)^2 + (30)^2$

1156 = 256 + 966

1156 = 1106

Rana Mujeeb 0303-6098695

Tarrellor . A.

Hence, it is a right-angled triangle.

2:- Here,

 $Hyp = c = \alpha^2 + b^2$

Perp. = b = 2ab

Base = $\alpha = \alpha^2 - b^2$

Rana Mujeeb Instructor 0303-6098695

According to phythologoras theorem, $c^2 = a^2 + b^2$

 $(a^2+b^2)^2 = (a^2-b^2)^2 + (2ab)^2$

 $(a^2)^2 + (b^2)^2 + 2(a^2)(b^2) = (a^2)^2 + (b^2 - 2(a^2)(b^2) + 4a^2b^2$

 $a^{4} + b^{4} + 2a^{2}b^{2} = a^{4} + b^{4} - 2a^{2}b^{2} + 4a^{2}b^{2}$

44 64+22 61= 44+64+2 a262

Hence, it is a right-angled triangle.

3:- Here,

Base= = 2

Prep = b = 8

Hyp. = C = 17

By phythagoras theorem,

c2 = a2 +b2

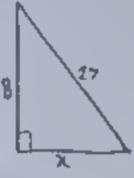
 $(17)^2 = (x)^2 + (8)^2$

289 = x2 + 64

289-64- 22

1225 = 1xx

x = 15



Rana Mujech Instructor 0303-6098695

mana Muieeb Instructor 08695

Instructor Mujeeb Rana Mujeeb 0303-6098695

Q6:-

eis Find value of 4xn?

In A ADC,

By phythagoras theorem,

 $c^2 = \alpha^2 + b^2$

$$(13)^2 = (5)^2 + b^2$$

Instructor Mujeeb
Rana Mujeeb
0303-6098695

In AABD,

By phythagoras theorem, $c^2 = a^2 + b^2$

$$(15)^2 = (x)^2 + (12)^2$$

Rana Mujeeb Rana Mujeeb 0303-6098695 7:--

Here,

Phythagoras theorem,

$$(x)^2 = (500)^2 + (300)^2$$

Rana Mujceb 303-6009605 Invinictor

Airpart

Rana Mujeeb

Instructor

0303-6098695

8 :- Here,

By phythagoras theorem,



Rana M.Ljech Instructor 0303-6098695

(vi) Review Exercise 15 0303-6098695

1:- Which of the following are true and which are not?

(i) In a right-angled triangle greater angle is 90. True

in In a right-angled triangle right angle is bo. False .

(m) In a right-angled triangle hypotenuse is a side opposite to right angle. True (iv) If a, b, c are sides of right-angled triangle with a as longer side then c2 = a2 + b2 . True ...

WIF 3 cm and 4 cm are two sides of a rightangled triangle, then hypotenuse is 5cm. True is If hypotenuse of an isosceles right triangle is sicm, then each of other side is of length 2 cm. False.

2-Find the unknown value in each of the following figures.

Rana Mujeeb 0303-6098695

According to phythagoras theorem,

$$c^{2} = a^{2} + b^{2}$$

$$(x)^{2} = (3)^{2} + (4)^{2}$$

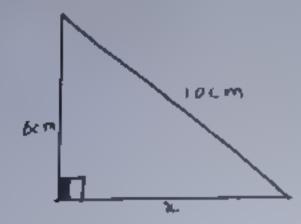
$$x^{2} = 0 + 16$$

$$x^{2} = \sqrt{25}$$

$$x = 5 cm$$

Instructor Nujeeb Rana Nujeeb 0303-6098695





According to phythagoras theorem,

$$((a)^2 = (x)^2 + (6)^2$$

Rana Mulech 0303-6003695

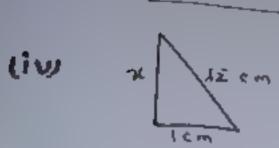
(હાં)



Rana Mujeeb Rana Mujeeb

According to phythagoras theorem,

Rana Mujeeb 0303-6098695



According to phythagoras theorem, $((2)^2 = (1)^2 + (1)^2$

$$2 = 1 + x^2$$

 $2 = 1 = x^2$

Rana Mujeeb Instructor 0303-60011115

Ranz Mujeeb Instructor 0303-6098635 "Theorem Related with Area.

Basic Concepts= (i) Area of a figure. in Interior of triangle. (iii) Triangular Region. ow Congruent Area Axiom. en Rectangular Region. (vi) Interior of Rectangle. win Altitude of triangle (viii) Altited of parallelogram. ex! Area of square. IXI Area of rectangle. Exis Area of parallelogram. (xi) Area . of triangle. Oin Important points. Drive Review Exercise 16.

ana Mujeeb 303-6098695

Rana Mujeeb 0303-6098695

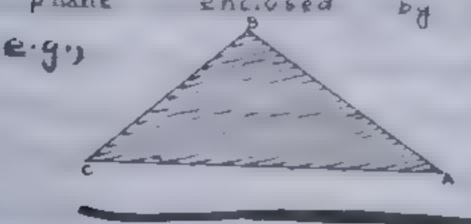
. Us Area of a figures

The region enclosed. by the bounding lines of a closed figure is called area of .. a figure. The area _ of _ a closed region is expressed in square units (say, say m, m2) i.e., or positive real number.

vis Interior of triangle = 0303-6018695

Instructor Rana Mujeeb

The interior of a triange is the part of the plane enclosed by the triangle.



Instructor Rana Mujeeb 0303-6058695

Wiis Triangular Region .-

4 triangular regien ... it the union of a triangle and its interior ie, the three line segments forming the triangle and its interior.

0303-6098695

in Congruent Area Axiom
If ∆ABC \(\sigma\) \(\text{Par}\),

then area of (region \(\Delta\) \(\Delta\) = area of (region \(\Delta\) \(\Delta\) \(\Delta\) \(\Delta\) \(\Delta\).

er, Rectangular Region:-

region is the union of a rectangular rectangle and its interior.

Rana Mujeeb

(vi) Interior of Rectangle :-

of a rectangle is the part

of the plane enclosed by

the rectangle

e.g.,

Instructor

Rana Mujeeb

0303-6098695

WAItitude of a triangle:

of a triangle is. taken as its base, the perpendicular to that side,

from the opposite vertex is called.

the altitude or height of a

e.g.,

wiiis Altitude of a Parallelogrami-

of a parallelogram is taken as its base, the perpendicular distance between that side and the side parallel to it, is called altitude or height of a parallelogram.

6.3.3

Rana Mujeeb

If one side

(ix) Area of a square:

enclosed by the boulding lines

of a squire is called

the area of squire.

In a square,

Area of a squite = Side X Side.

Rana Muje 0303-60986

ist Area of a rectangle:-

The region :
enclosed by the bounding lines of:
a rectangle is called the area of
of rectangle.

In a rectangle,

Area of rectangle = Length X width.

(xi) Area of a triangle :-

enclosed by the bounding lines of a triangle is called the area of triangle.

In a triangle,

Area of triangle = 1 x Base X Altitude

(xii) Area of parallelogram :-

The region

enclosed by the bounding lines of

a parallelogram is called the orea

of parallelogram. Instructor

Rana Mujeeb

0303-6098695

. Area of parallelogram = Base X Altitude.

. (xif) Important points :-

- Paralle lograms on the same base and between the same parallel lines (or of the same altitude) are equal in area.
- Parallelograms on the equal bases and having the same (or equal) altitude are equal in area
- Triangles on the same base and of the same (ie, equal) altitudes are '- equal' in area.
- equal altitudes are equal in area.

 Instructor

 Rant Majee

wive Review Exercise 16:- 0303-609863

1:- Which one of he following are true and which are false?

enclosed by bounding lines of closed

figure True

tiv Similar figures have same area. Fine
tive Congruent figures have same area. Fine
tive A. diagonal of a parallelagram dissided.
it into two non-congruent triangles.

False

Rana Mujeeb 0303-6098695 Altitude of a triangle means .. perpendicular from vertex to the ., opposide side (base). True (vi)Area of a parallelogram is equal to the product of base and height. True. 2:- Find area of the following -, (i) 3 cm Instructor Rana Mujeeb 0303-6098695 we know that of rectangle = Lackgth x Width = (6) (3)

Instructor Rana Mujeeb 0303-6098695

= 18 cm2

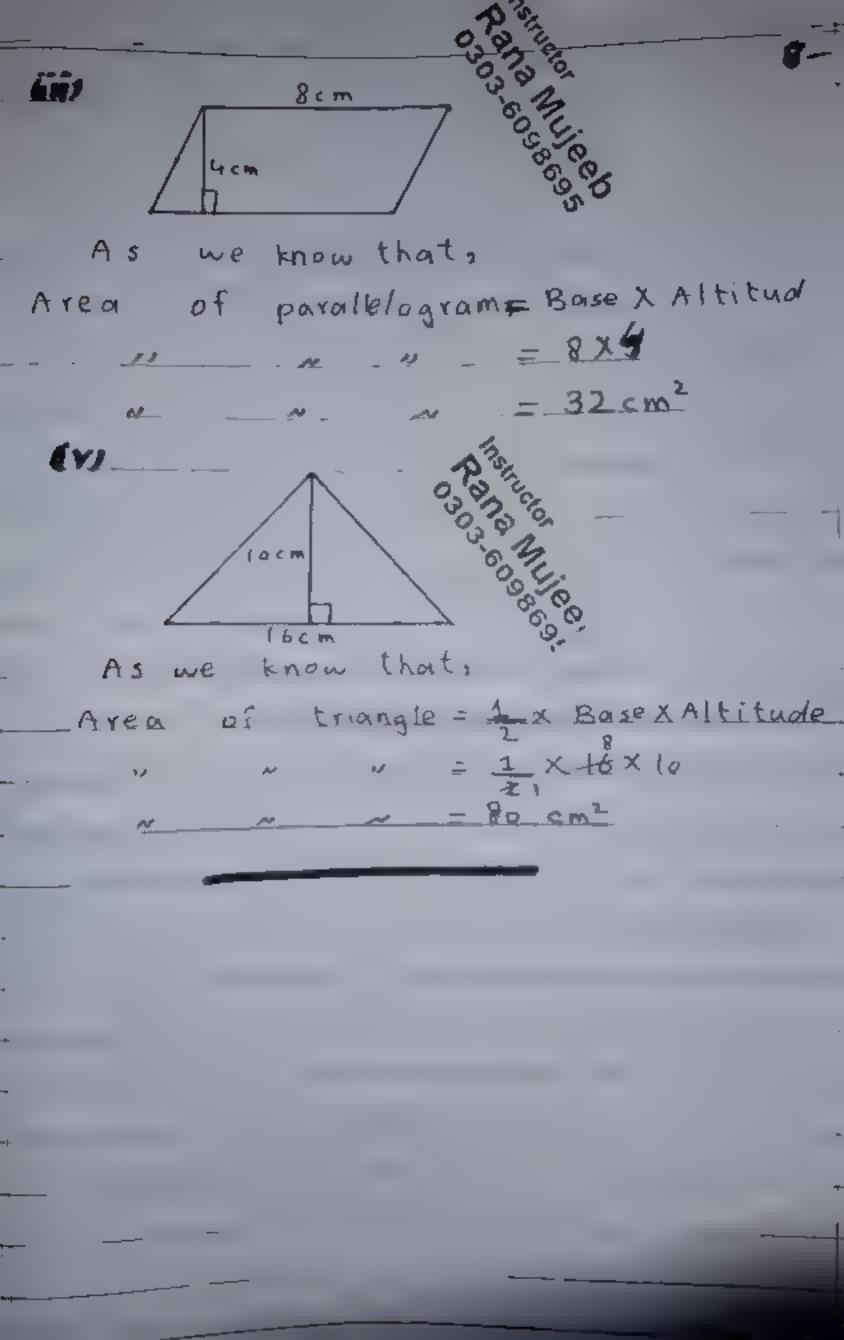
As we know that,

Area of square = sido x side

" " = 4 x 4

" " = 16cm²

Rana Mujeeb 0303-6098695



Chapter No 17: "Practical Geometry Triongles instructor

Instructor Rana Mujeeb 0303-6098695 Rana Mujeeb 0303-6098695

Basic Concepts

i) Angle Bisector.

Perpendiculor Bisector.

Michigan.

AND Altitude.

V) Concurrent lines & Point of concurrency

vy centroid.

Rana Wujeeb

Visit Orthocentre 0303-6098695

ixx Circum-Centre.

W Observe that.

Ki) Ex 17.1 (complete).

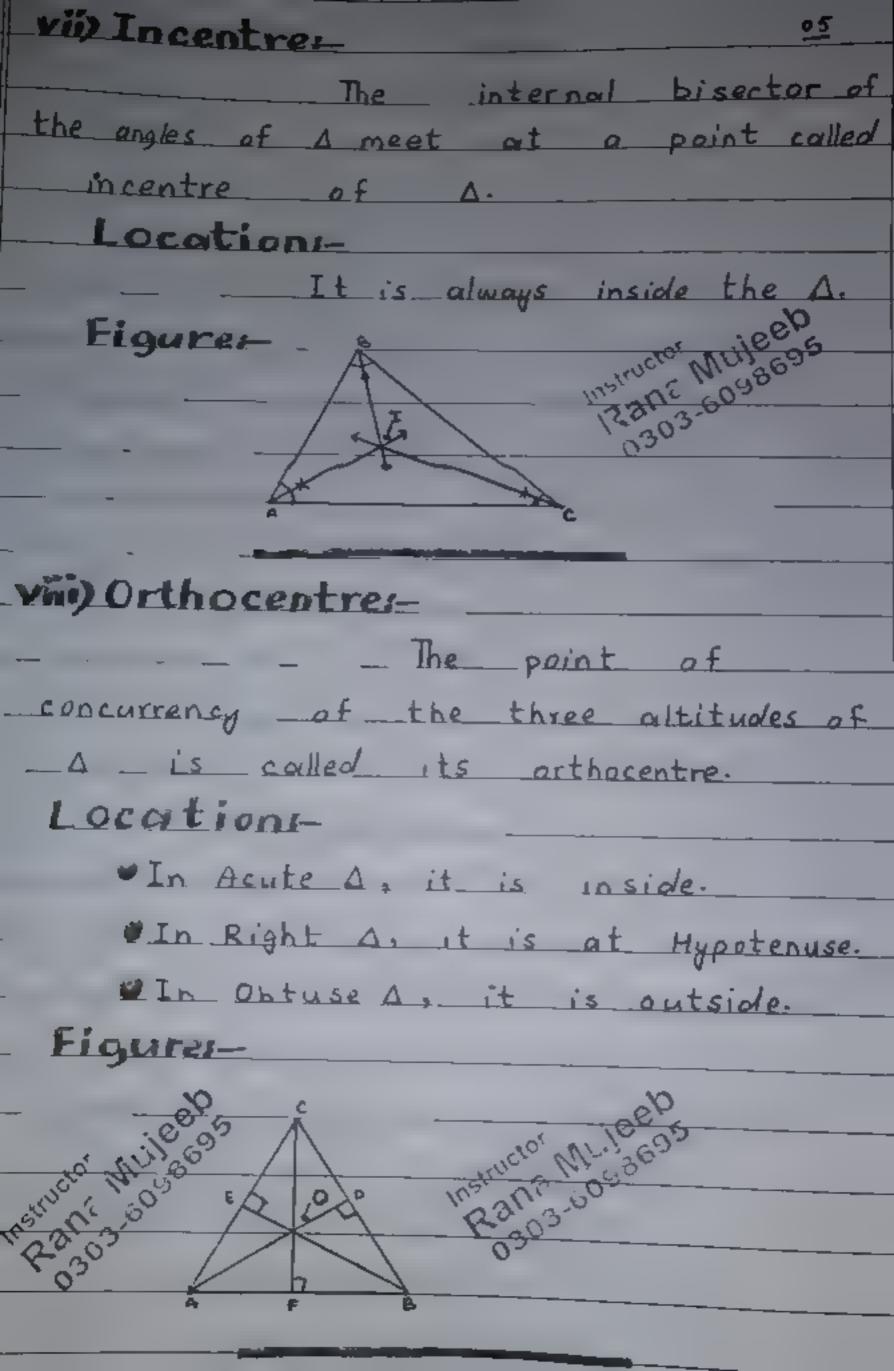
xiii) Ex 17.2 (complete).

x 17.3 (Q1 () Sii Only).

with Review Ex 17.

i) Angle Bisectori-- Angle bisector is the ray which divides an: angle into two equal parts. Rane Mr. Jeeb ii) Perpendicular Bisector-A line & is called perpendicular bisactor of line segment if l is perpendicular to the line segment and passes through its mid-point. Instructor Milites Instructor Milleges ±m

V)Concurrent lines & Point of _concurrency:-Three or more than three lines are social to be concurrent, if they all pass through the same point. The commor point is called point of concurrency Instructor Mileebe Here, P 15 a point of concurrency. wir Centroid: The point where the three midians of A meet is called centroid of A Location: It is always inside the A. Figure:-Instructor Miles Beas

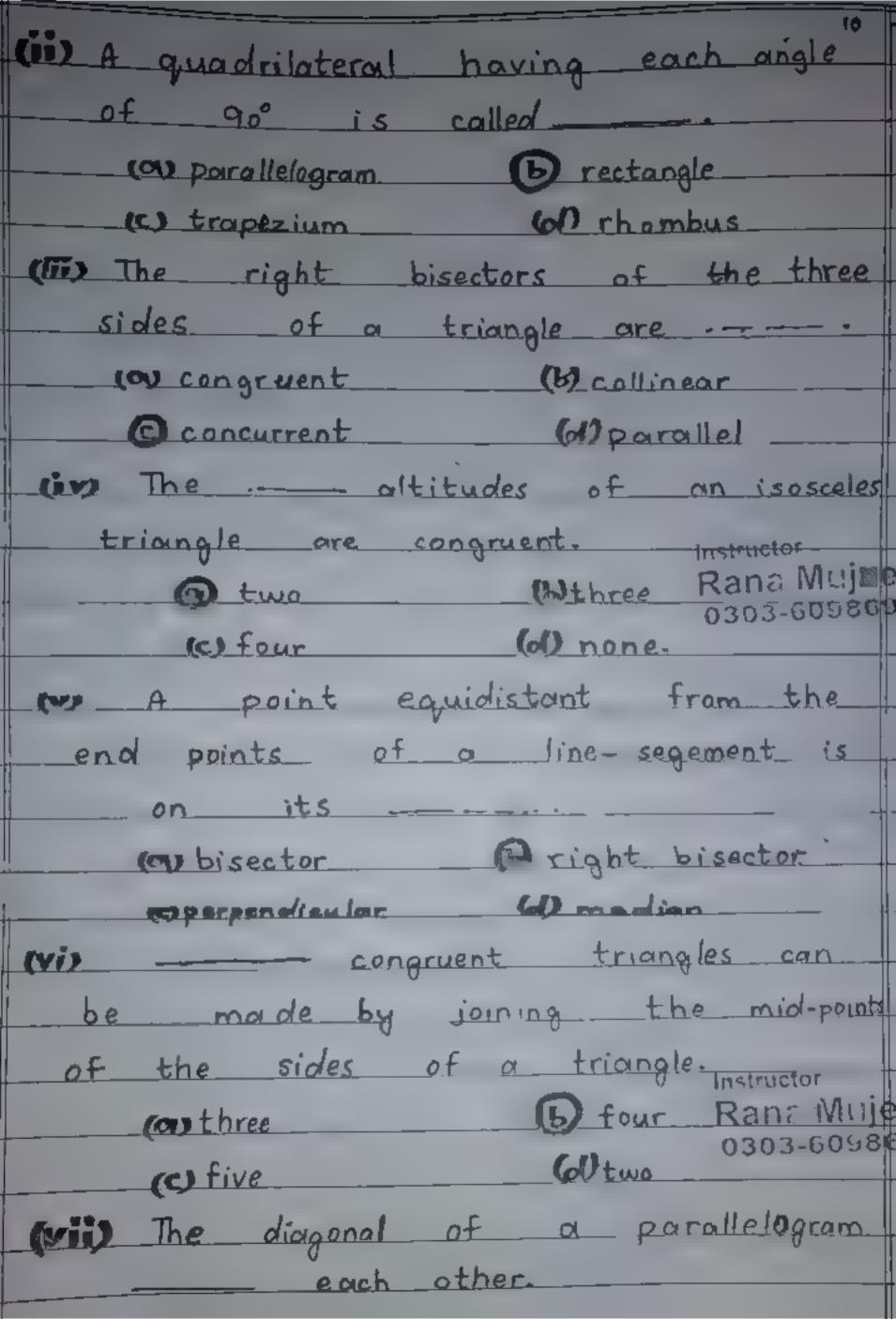


m) Observe that

As APC, ADC stand on the same base AC and b/w the same parallels AC and PD. Hence $\triangle APC = \triangle ADC$ APC+DABC = DADC + DABC or DPBC=quodilateral (ARCD)

(iii) These two ares cut each other at point C. Join Cto A & C to B. (N) Draw on arc of radius 3.8cm with centre c and dow on arc of radius 2.8cm with centre A. (x) These two ares cut each other at point D. Join D to C and D to A to complete quidilateral ABCD. Wil Through D. draw DPILAC meeting BA produced at P. (vii) Join P to C. Hence DPBC is required a and its <u>area</u> is equal to quadilateral ABCD. xiv) Review Ex 17 2. Fill In the blanks to. make startement true. is The side of a right angled triangle apposite to 70° is colled. Hypotenuse. 11) The line segment joining a vertex of triangle to mid-point of its opposite side is called a medicun.

in A line drawn from a vertex of a triangle which is Perpendicular to its opposite side is called on altitude of triangle. and The bisector of three angles of a triangle are concurrent. W) The point of concurrency of the right bisectors of the three sides of the triangle is equidistant from its vertices. (VI) Two or more triangles are said to be ___ similar __ if they __ are equiangular and measures of their corresponding _ sides _are Proportional (VII) The altitudes of a right triangle are concurrent at the Vertex of the right angle. 2. Multiple Choice Questions. Choose the correct answer. (i) A A having two sides congruent is called _ couscalene (b) right angled disosceles. (c) equilateral



xi)

Ex 17.1

(i) mAR = 3.2 cm, mEE = 4.2cm, mCA = 5.2cm

Instructor Allifeess

Rang Go Jacob Service

Rang Go Jacob Service

C 6-2 cm A

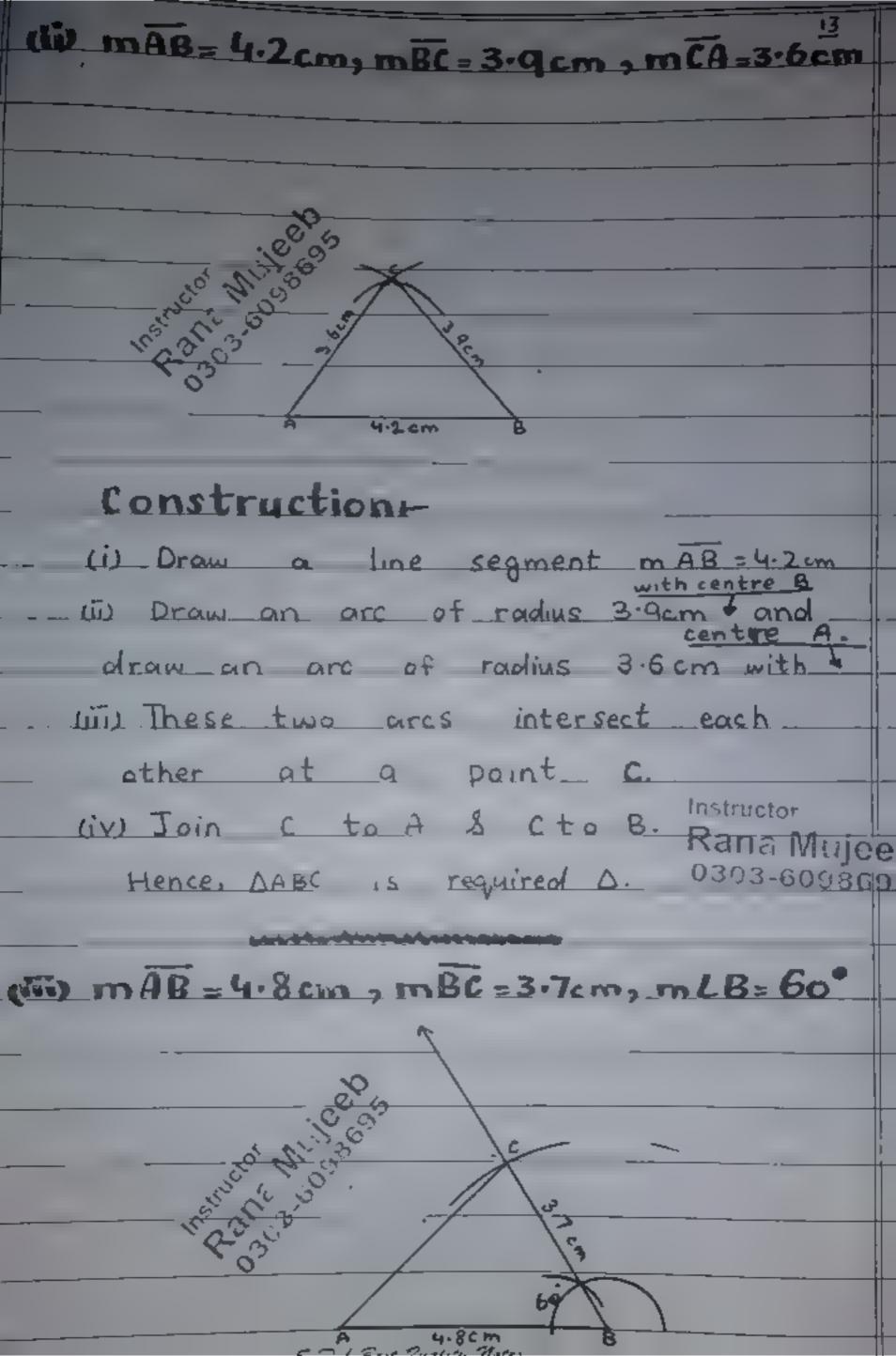
Construction Ran: W...jeeb

(i) Draw an arc of radius 4.2cm and
draw an arc of radius 2.2cm

(iii) These two ares intersect eath other at a point B.

((v) Join B to C and B to A.

Hence, DABC is required D.



Construction-

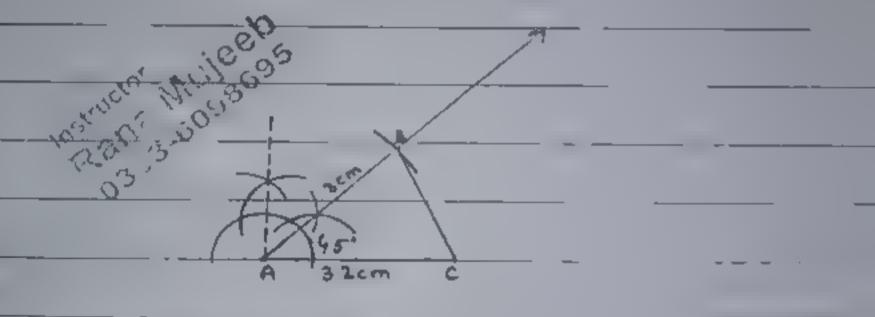
- (i) Draw a line segment mAB=4.8cm
- (ii) Make an angle of mLB = 60°
- (III) Draw an arc of radius 3.7cm

with centre B.

(iv) Join C to A.

Hence, DABC is required A.

(iv) mAB= 3cm, mAC=32cm, mLA=45



Construction:-

- (i) Draw a line segment mAC = 3.2cm
- (ii) Make an angle of mLA = 45°
- (iii) Draw an are of radius 3cm with meandctor.

Rana Mujeeb centre A.

0303-6098695 tio Join 8 to C.

Hence, ΔABC is a required Δ.

00 mBC = 4.2cm, mCA = 3.5cm, m/c=75° Construction: (i) Draw a line segment m BC=4.2cm (ii) Make an angle of mLc = 75° (III) Draw an arc of radius 3.5cm with centre C. (ix) Jain A to B. Hence, DABC is required A. (vi) mAB = 2.5 cm, mLA=30°, mLB=105° Rana Mijech Instructor -In'structor Rana Mujeel 0363-6093695 0303-609869

Construction

(i) Draw a line segment mAB = 2.5cm.

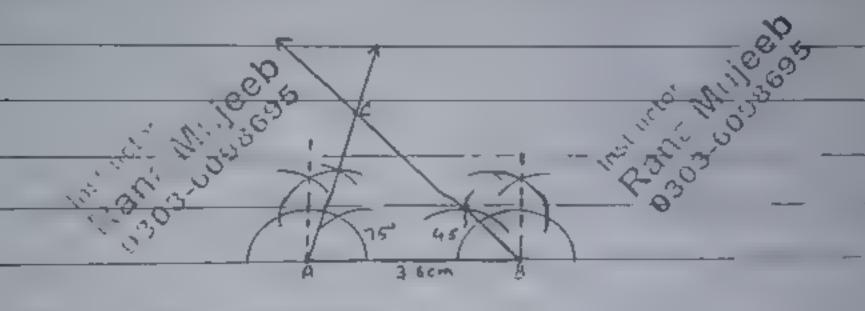
(ii) Make an angle of mLA = 30°

(iii) Make an angle of mLB = 105°

(iv) These rays intersect each other at a point C to complete Δ ABC.

Hence, ΔABC is a required Δ.

(Vii) m AB = 3.6 cm, m/A = 75° 1 m/B= 45°



Construction :-

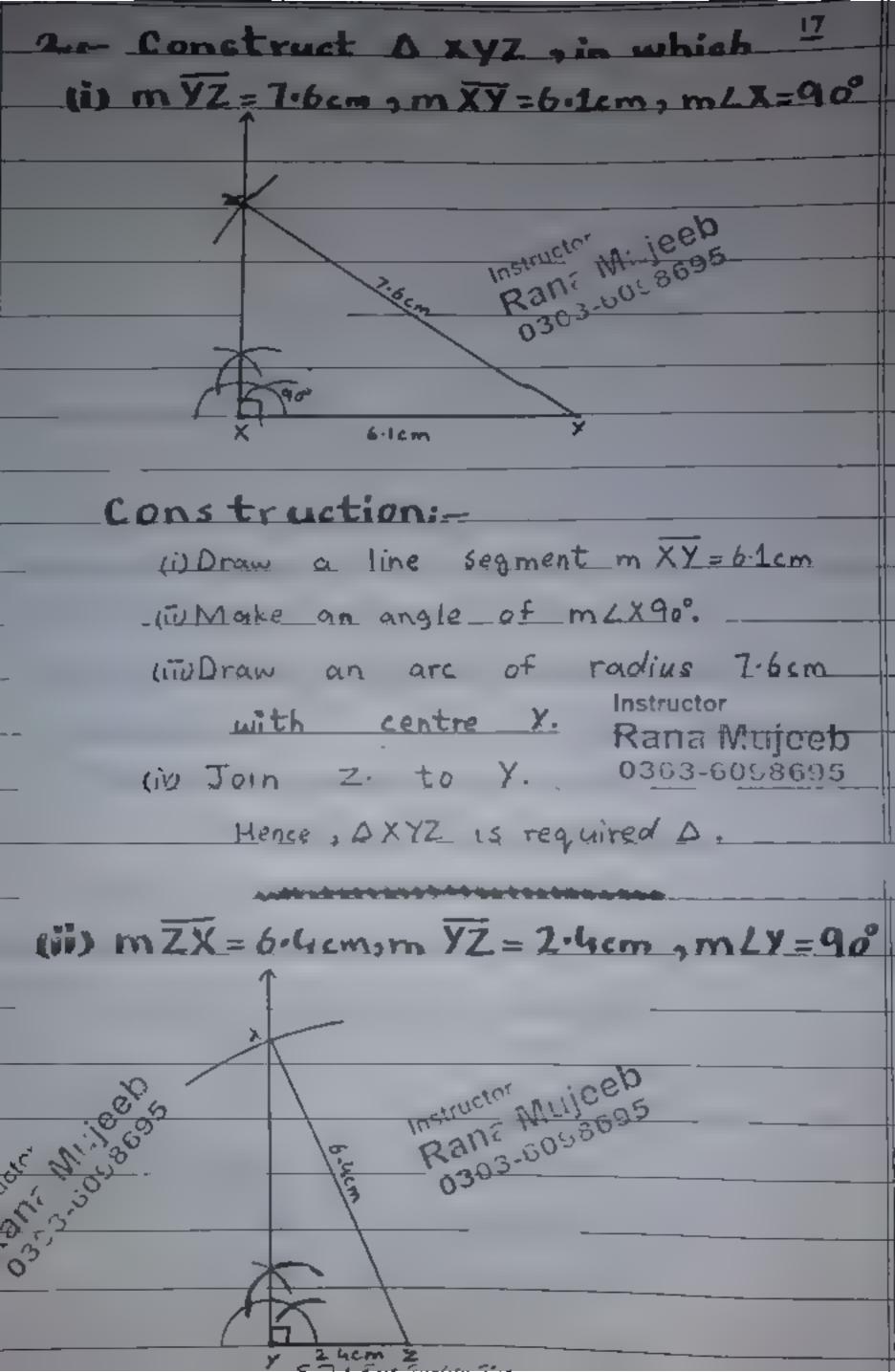
(i) Draw a line segment mAB = 3-6cm

(ii) Make an angle of mLB = 15°

(iv) These ray intersect each oth

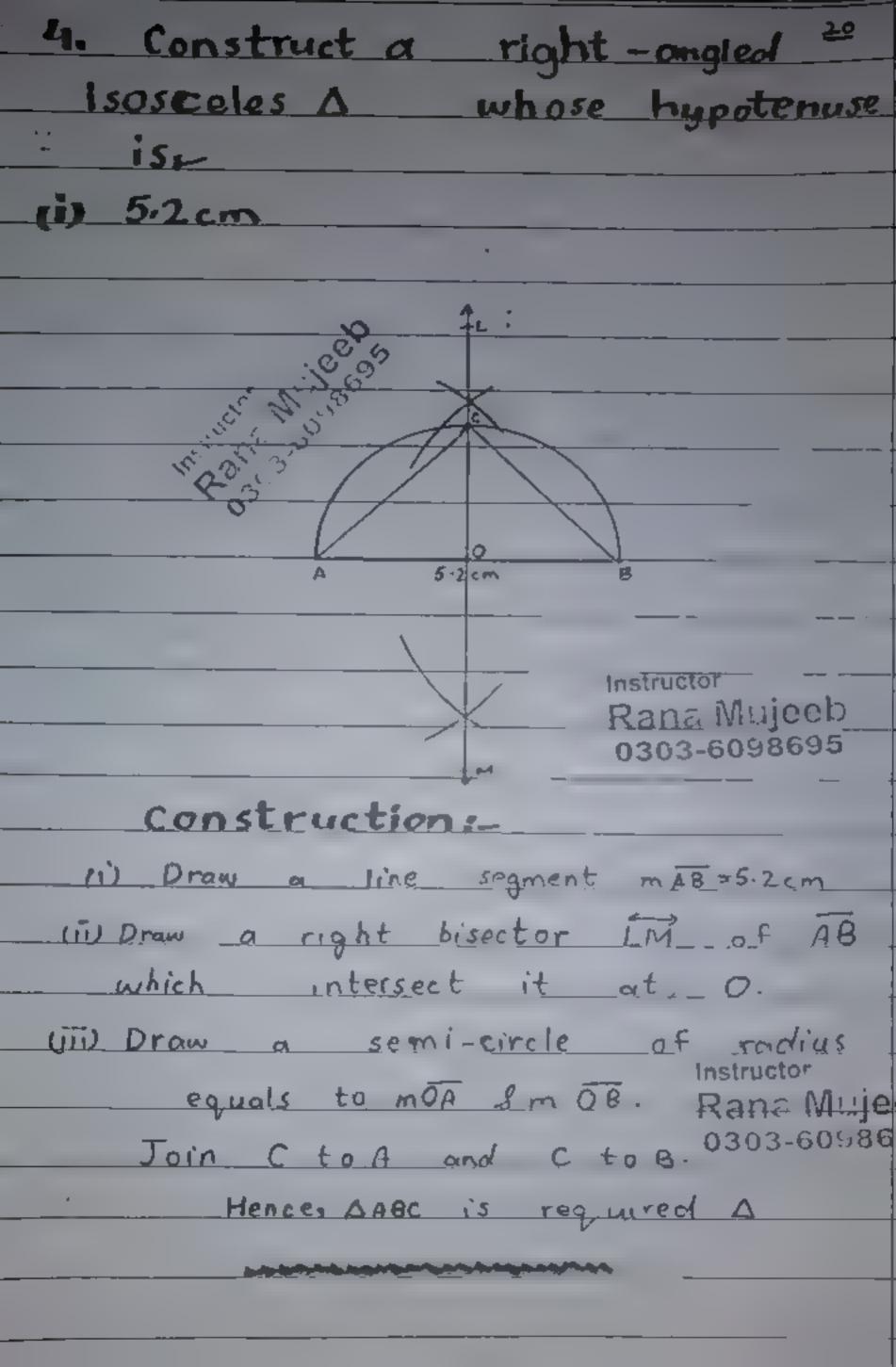
at point C to complete DABC.

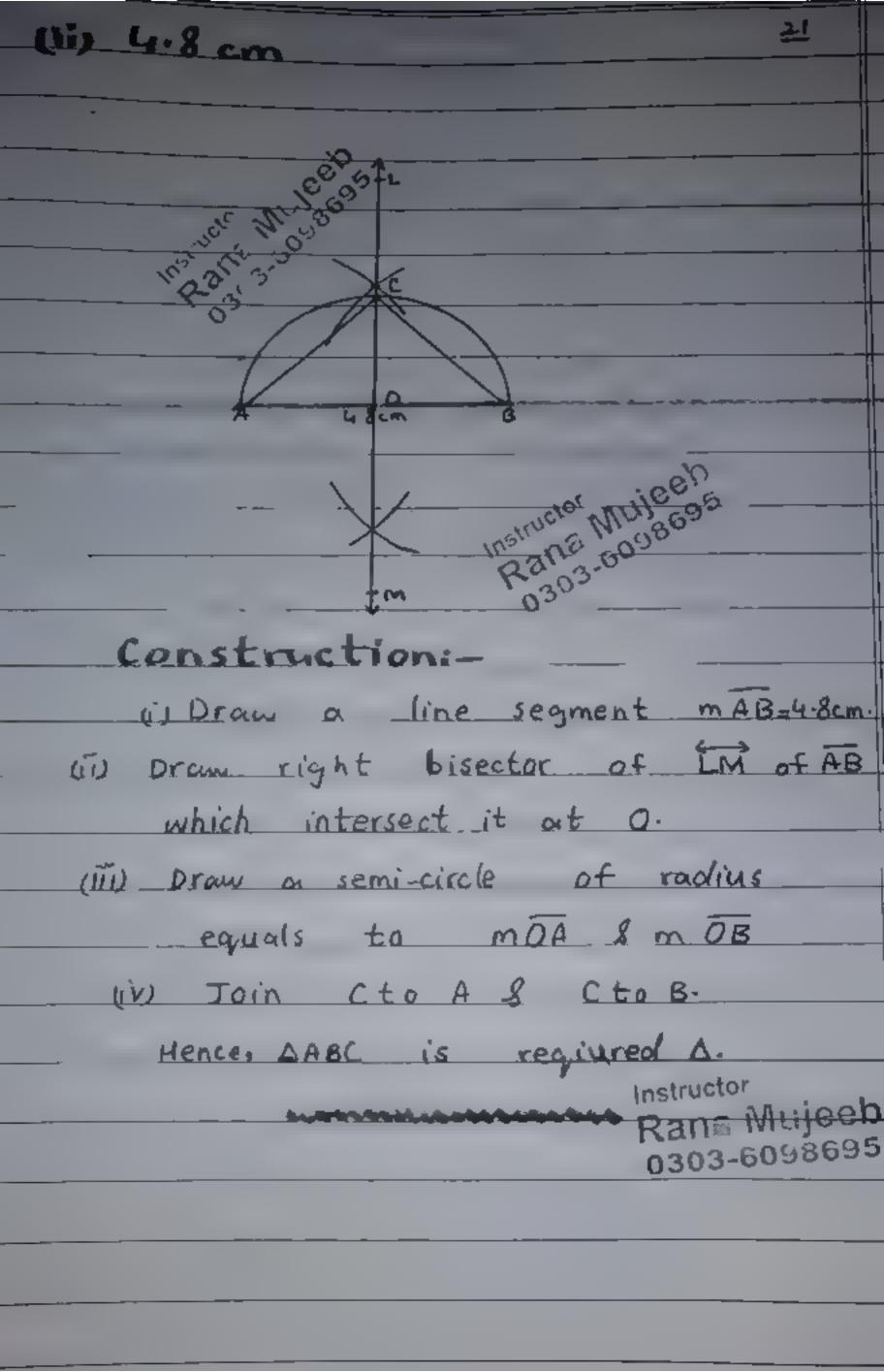
Hence, DABC is required D



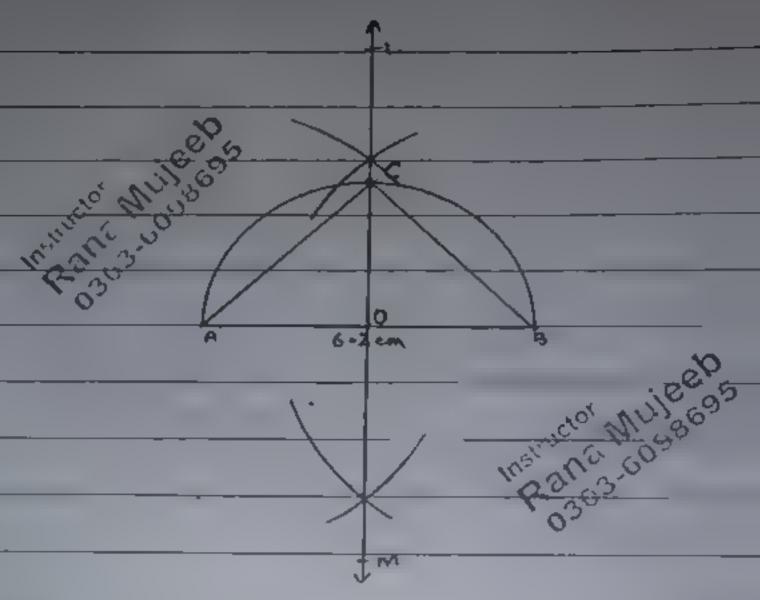
(i) Make an angle of mLZ=900 (in Draw an arc of radius 5.5cm Rana Mujeeb (iv Jan Y to X. 0303-6098695 Hence, AXYZ is required 1

3 " construct a right-angled A measure of whose hypotenuse is 5cm and one side is 3.2cm. Harrieto, Millecon Ranz Mujeeb 0303-0098695 Construction .-(i) Draw a line segment mAB = 5cm (ii) Draw a right Bisector LM of AB which intersect it at o. (iii) Draw a semi-circle of radius equals to mOA and mOB. (IV) Draw on arc of radius 3cm from Instructor centre A. Toin Atoc & B to C Rana Minjon Hence, DABC is required 1.





(iii) 6.2cm



Construction -

ii) Draw a line segment mAB = 6.2cm

OI) Draw right bisector im of AB

Which bisect it at o.

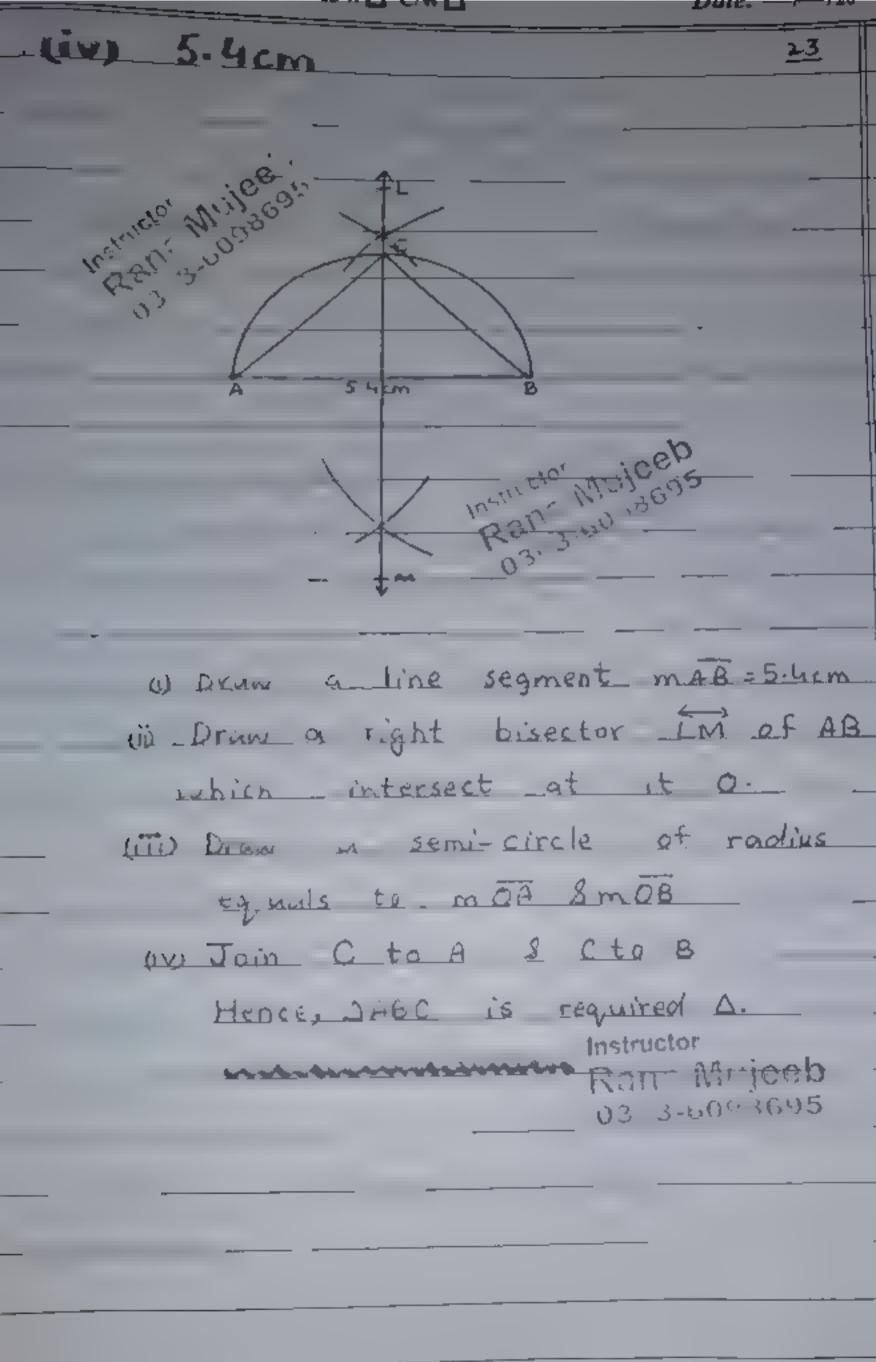
(iii) Draw a semi-circle of radius

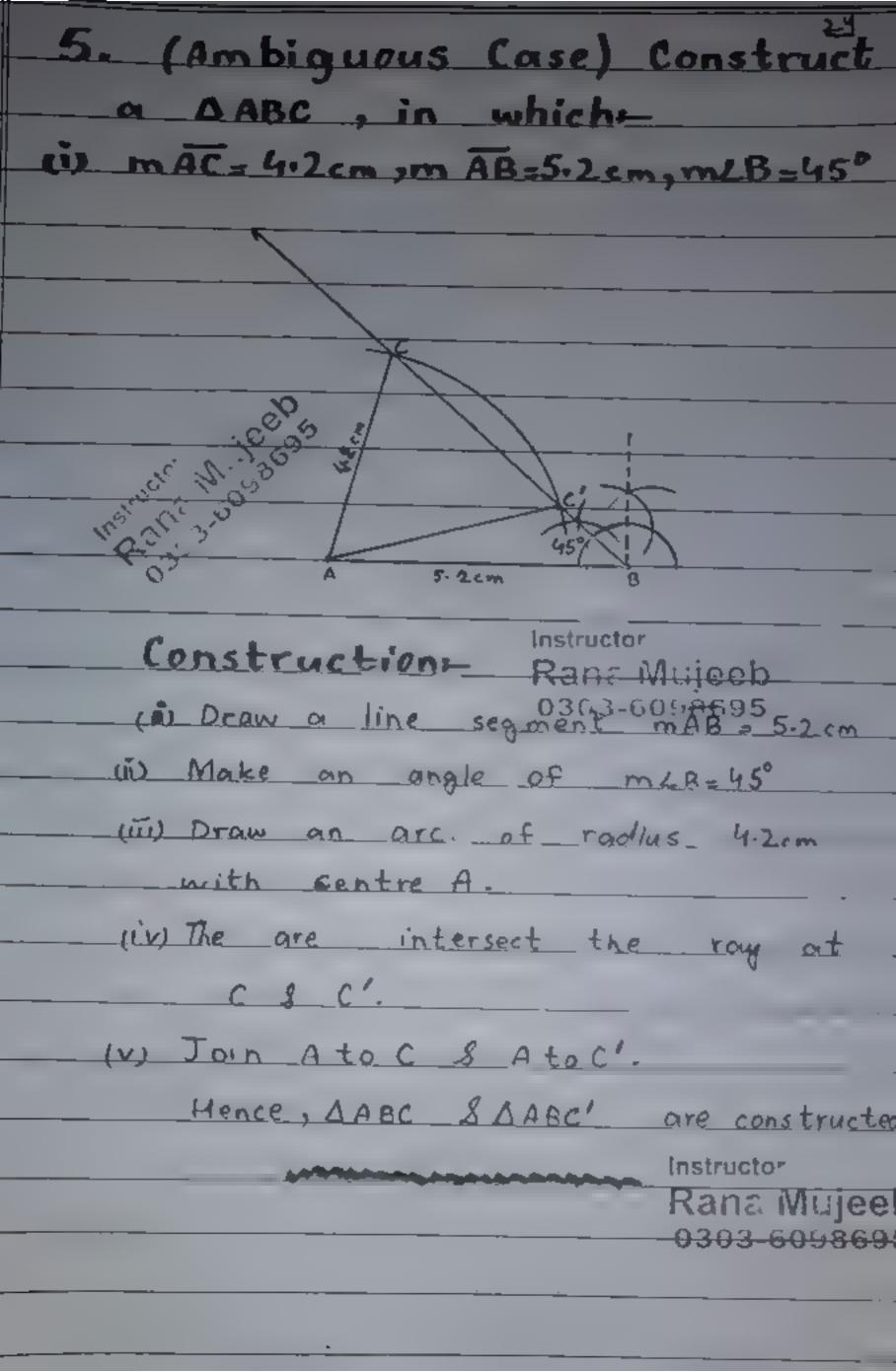
equals to mOA smOB

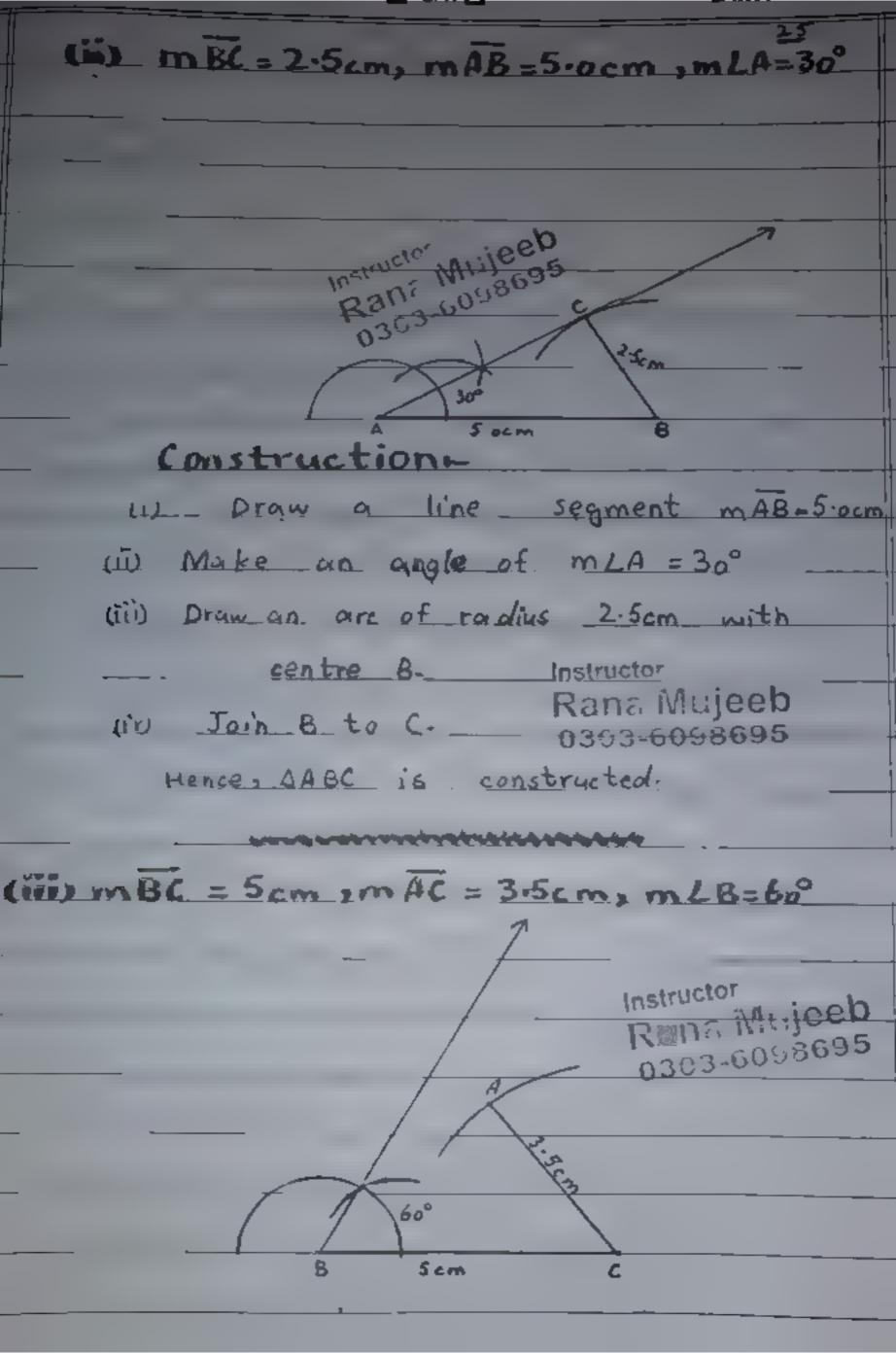
(iv) Join C to A and Cto B.

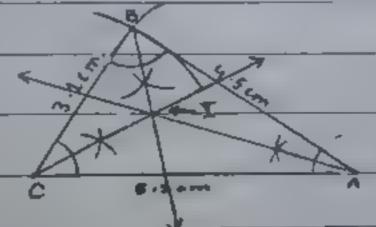
Hence, DABC is required A

Rana Mujeeb 0303-6098695





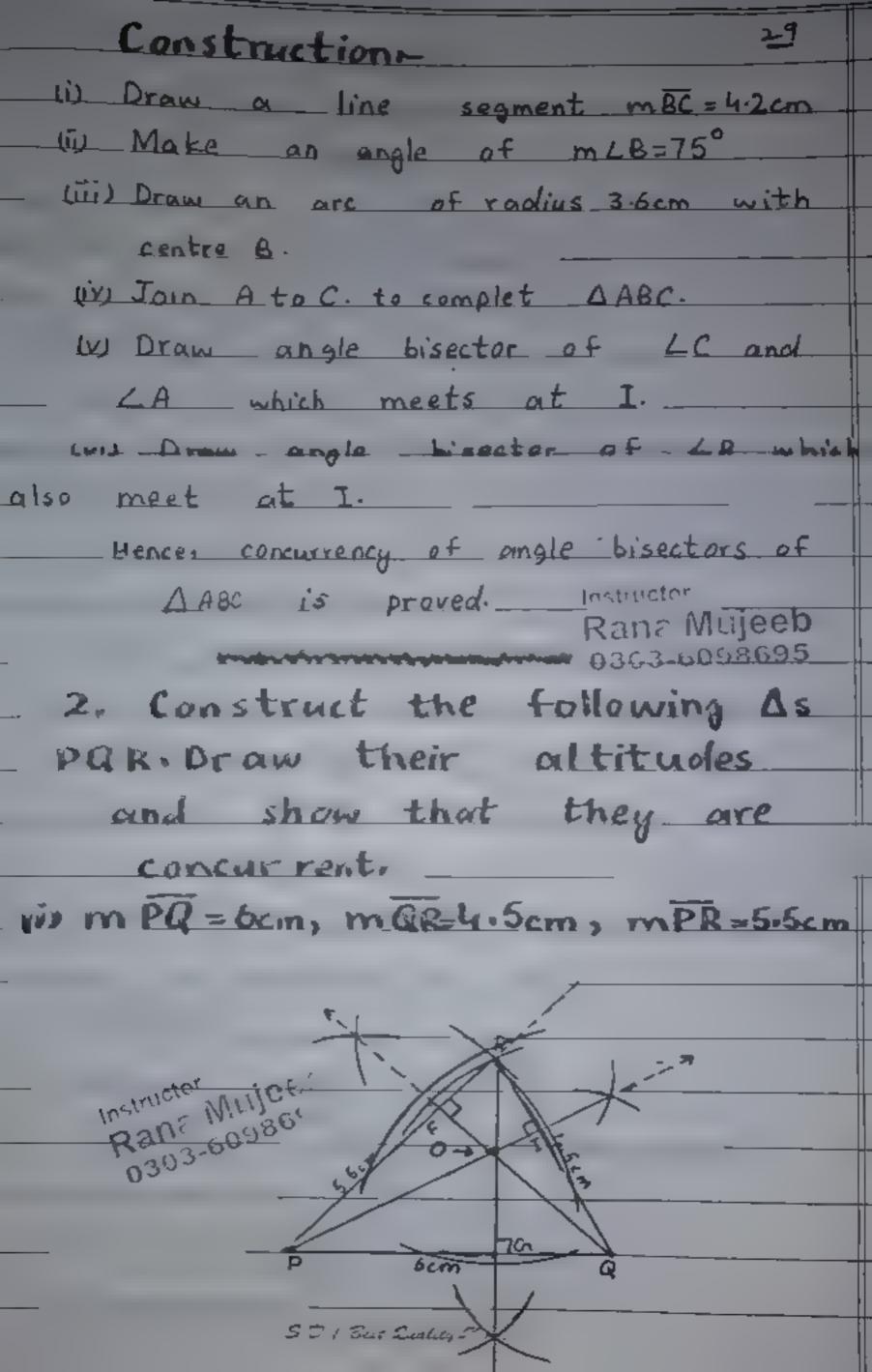


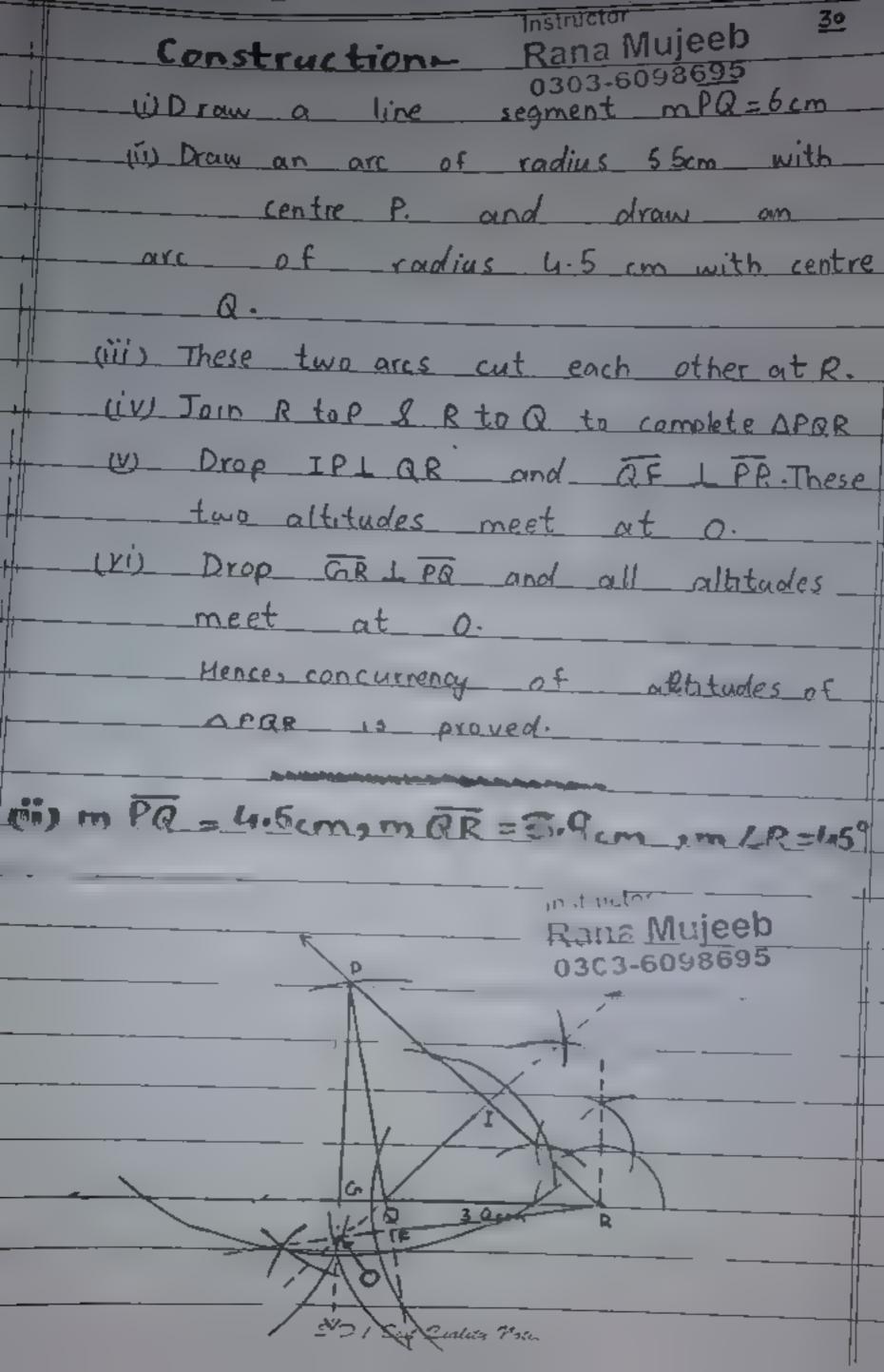


Constructionin Draw a line segment mcA =5-2cm WI Draw an are of radius 4.5cm from centre A. (iii) Draw an are of radius 3.1cm from centre C. UV) These two arcs cut each other at 8. W) Join AtoB and B to C ._ to complete A ABC. (vi) Draw angle bisector of LC and LA which meets at I. (viv Drum ungle bisector of LB which also meet at I. Hence, concurrency of angle bisectors of DABC is proved. 112 m AB = 4.2 cm, m BC=6cm, m CA = 5.2cm 0303.609

	78
Construction	
(i) Draw a line segment = 5.2 cr	n
(ii) Draw an arc of radius 6cm	with
centre C.	
wii Draw an arc of radius 4.2cm	with
centre A.	
UN These Btwo arce cut each ou	ther
at B.	
W Join B to C & B to A to comp	lete
ΔΑΒζ	
(vi) Draw angle bisector of 20 8 LA	which
meets at I.	
viv Draw angle bisector of LB which	01/50_
meet at I.	
Hence, concurrency of angle bisectors	
of OABC is proved.	
(iii) mAB = 3.6cm, mRC = 1.2cm, m/R	=75°

Ran Wallech Instructor Rana Majeeb 0303-6098695





Date: ---- (20-Construction 31 tis Draw a line segmen mak = 39cm like Make an anole of milk=45° VIII Druw on arc of radius 4 5cm with centre a (i) Jain Q La P. La complete DPQR. W Drep QILPR and RF LPQ . These two altitudes meet at a. WID DIOD PG LQR and all altitudes meet at Q. Hence, concurrency of altitudes of In Fuctor SPAP is proved: "Rana Muleeb 3-6098695 (111) mRP = 3.6cm, mLQ = 30, mLP=105 m L R + m L Q + m L P = 180° m LB + 31° + 105° = 180° m L R+ 135° = 180° m LR = 180-136° Ran- Wirjeeb rn LR = 45% 035 FUC 3695

3. Construct the following As

ABC Drow the perpendicular

bisectors of their sides and

verify their consurroney Do

they meet inside the A?

i) mAB = 5.3cm, mLA=45,mLB = 30°.

Construction-

(1) Draw a line segment mAB=5.3cm.

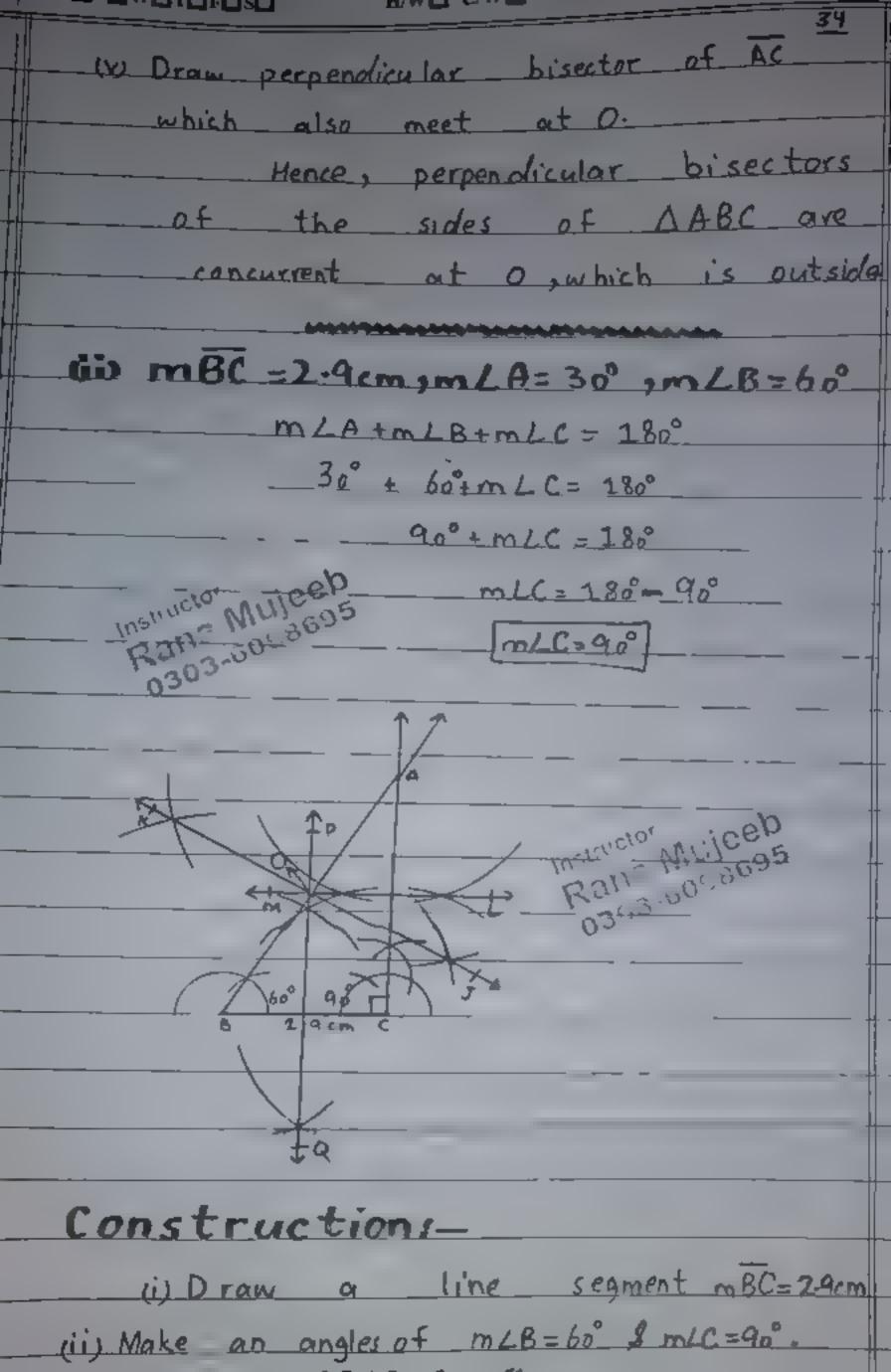
(1) Nlake an angles of mLA=45° &

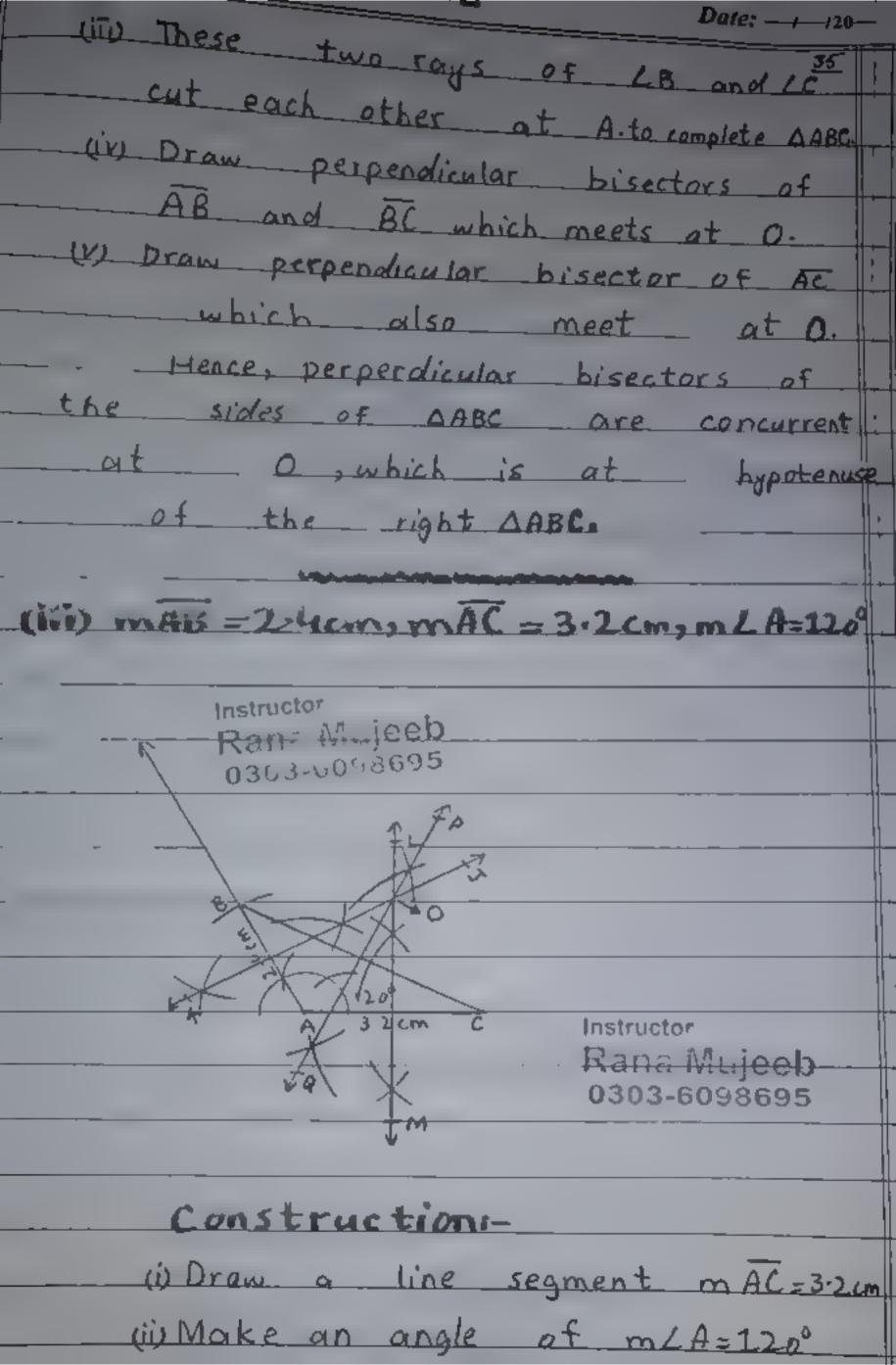
(iii) These two rays of LA and.

LB cut each other at C. to

(iv) Draw perpendicular bisector of

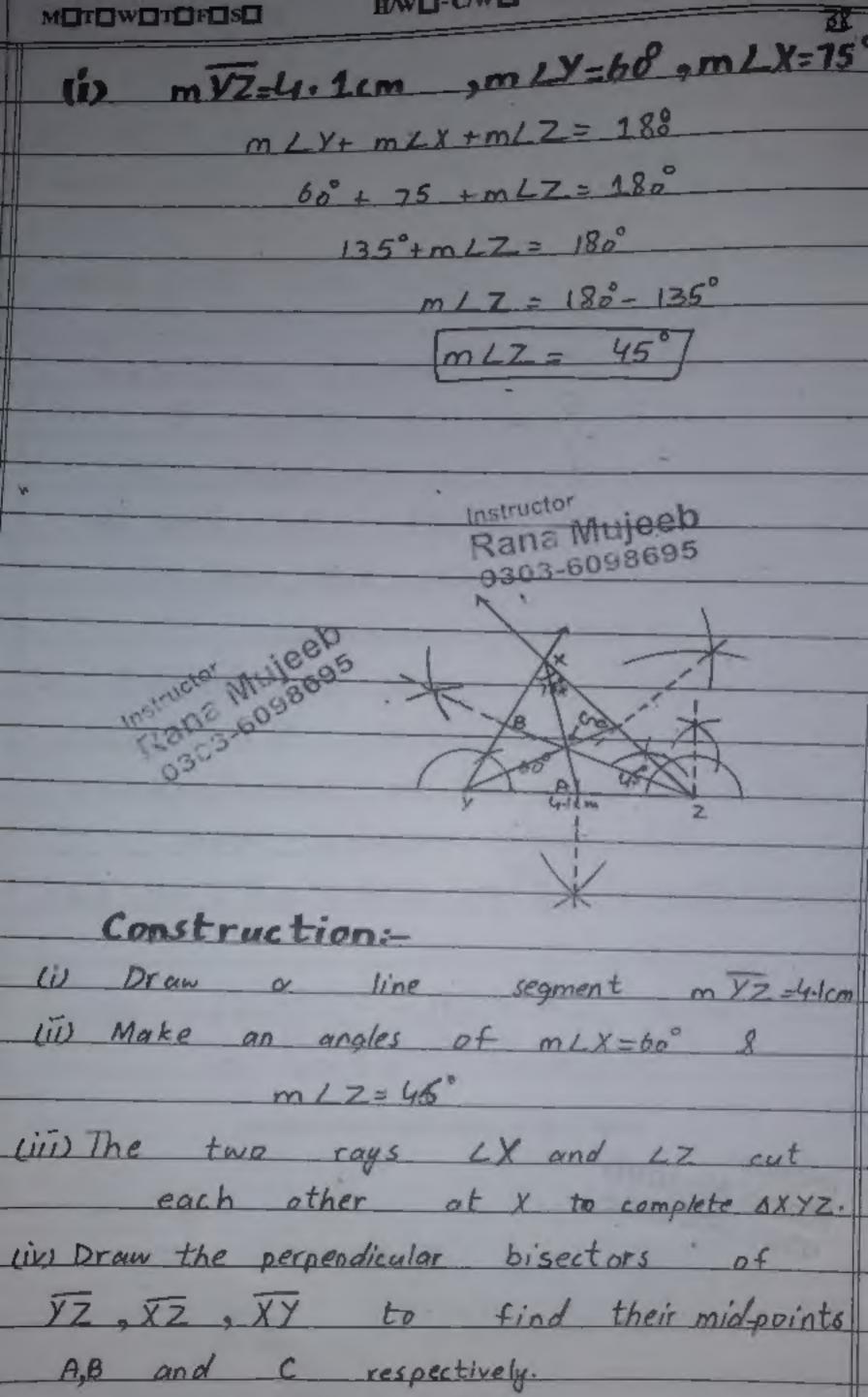
AB and BC which meet at Q.

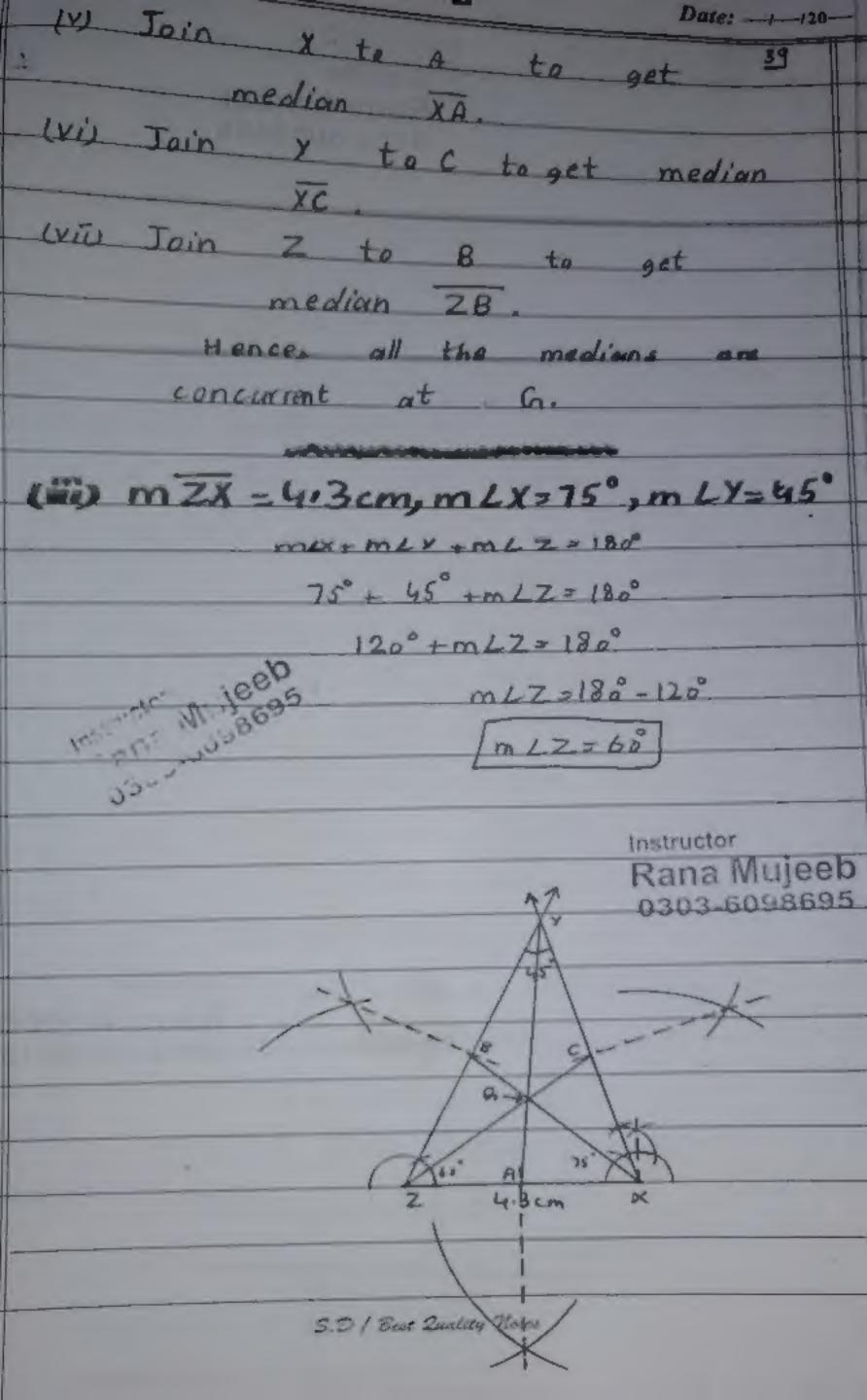




(iii) Draw an are of radius 2.4cm with centre A. (iv) Join A to C to complete DABC. (V) Draw perpendicular bisectors of AB and BC which meets at 0. Wil Draw perpen dicular bisector of AC which also meets at O. Hence, Perpendicular bisector of the sides of AABC are concurrent at a which is outside. からからなるとうとうとうとうかん 4. Construct the following As XYZ, Oraw their three medians and show that they are consurrent: (11) mxy = 4.5cm, myz-3.4cm, mZx =5.6cm Instructor Rana III teeb 03- ----098695 Instructor Rana Mujeeb 0313-6058695 5-6 cm t Invaling Notes

Construction Rana Milleeb 120-0303-609869537 (i) Draw a line segment mZX = 5.6cm (ii) Draw an one of radius 4-5cm with contre x 3 draw an arc of radius 34cm with centre Z. (iii) These two ares cut each other (iv) Join Y to Z and Y to X to complete A XYZ. (x) Draw perpendicular bisectors of 2x, 7x and 29 to find the miolpoints as A, B, and C respectively. (vi) Join Y to A to get median Y A . (vii) Join 2 to B to get median (viii) Jain X to C to get median XC. Hence all the medians are concurrent out on. Rana Mujeeb Instructor 0303-6098695





Rana Muieeb 0303-6098695 in Draw a line segment m ZX = 4.3cm Liv Make an angles of m/7=60° 8 m/ K=75°. (iii) The two rays _____ LZ and Lx cut each other at y. iv) Draw perpendicular bisectors of ZX, YZ and XY to find their mid-point A, B & C respectively. W) Join 2 to C to get median ZC. wij Join X to B to get median XB. (VII) Jain Y to A to get median YA. Hence, all the medians are concurrent at G. Instructor
Rana Mujeeb -- 0303-6098695